

Modeling weather and stocking rate effects on forage and steer production in northern mixed-grass prairie



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ABSTRACT

Stocking rate (SR) is the primary management factor that influences livestock gains, plant community changes and forage production, as well as economic returns for livestock producers. More effective stocking decision making by ranchers in the semi-arid northern mixed-grass prairie requires clearly understanding forage production and yearling steer weight gain (SWG) responses to SR and high weather variability. The objectives of this study were to: (1) test the Great Plains Framework for Agricultural Resource Management-Range (GPFARM-Range) model for predicting forage production and SWG under three experimental SR treatments and long-term weather conditions on semiarid northern mixed-grass prairie in southeast Wyoming, USA; and (2) quantify the threshold responses of forage production and SWG to SR and the yearly weather variability across years using long-term simulations with SR higher than those experimentally evaluated. We improved upon the GPFARM-Range model to simulate peak standing crop (PSC) and SWG for three experimental SR treatments (low, moderate and high; 0.20, 0.33 and 0.44 steer ha⁻¹, respectively) from 1982 to 2012 at Cheyenne, Wyoming, USA. The improved model accurately predicted the effects of SR on PSC and SWG across years (root mean square errors from 355 to 387 kg ha⁻¹ for PSC and from 12.8 to 14.2 kg head⁻¹ for SWG). We ran the model with long-term weather data and 50–300% higher SR (0.66–1.76 steer ha⁻¹) than the high SR experimental treatment. Differential responses of predicted total intake of digestible nutrients (quadratic increase) and metabolic maintenance (linear increase) to these higher SR resulted in a quadratic increase of predicted SWG with SR and high yearly variability at high SR levels. The financially-optimum SR with highest profits was reduced to 0.33 steer ha⁻¹ for dry or normal seasons and 0.44 steer ha⁻¹ for wet seasons. Such reduced SR can also benefit land conservation with high PSC and low harvest efficiency. The moderate SR with 25% harvest efficiency was determined between 0.22 and 0.33 steer ha⁻¹ for dry or normal seasons, or between 0.33 and 0.44 steer ha⁻¹ for wet seasons. These results provide useful direction for selecting an effective SR to achieve high economic net return with lower yearly variability (risk) and reduced likelihood of rangeland degradation.

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1. Introduction

Seasonal weather variation and stocking rate (number of animals per unit land area for the grazing season, SR) influence forage production (Biondini et al., 1998; Derner and Hart, 2007), cattle weight gain (Derner et al., 2008b; Reeves et al., 2013a,b, 2014), and the economic net returns (Hart et al., 1988; Manley et al., 1997) in semiarid rangelands. For example, forage production

and livestock weight gain responses to SR differ between drought and wet conditions (Gillen and Sims, 2006), across locations and climates (Smart et al., 2010), and with different plant communities (Derner and Hart, 2007; Patton et al., 2007; Reeves et al., 2014).

Greater spring precipitation (Derner et al., 2008b; Reeves et al., 2013a,b, 2014), as well as cool springs (Reeves et al. 2013a, 2014) can increase livestock weight gains in northern mixed-grass prairie. Additionally, livestock weight gains were more sensitive to seasonal weather influences as SR increased (Reeves et al., 2013b, 2014). These results can be used by land managers to adjust SR levels to seasonal weather variability. However, clearly understanding

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the SR effect on the variability of forage production or livestock weight gain due to weather variations is needed to better match cattle forage demand to forage availability across seasons and reduce enterprise risk and land degradations.

Field studies have generally evaluated only a few SR levels due to limitations in experimental design (i.e., adequate replication and logistical difficulties associated with grazing studies) and concerns about poor animal performance when SR levels are high. However, system models provide the ability to extend field experimental results by simulating effects of various SR on forage production and livestock weight gain for various weather conditions. Furthermore, system models could explore the threshold effect of SR on forage production and livestock weight gains across a wide range of weather conditions, which can assist in stocking decisions by ranchers.

Many process-based models have been developed to simulate forage growth and livestock production, such as GRAZPLAN (Freer et al., 1997) and AgMod (Johnson, 2013) in Australia, and the Farm Assessment Tool (FASSET, Berntsen et al., 2003) in Denmark. These models were mainly developed for the local conditions, such as pasture species, and grazing and fertilizer management options (Snow et al., 2014). In the Northern Great Plains of U.S., the Great Plains Framework for Agricultural Resource Management-Range (GPFARM-Range) model was developed by USDA-Agricultural Research Service to address simultaneous influences of weather, soils, and various SR levels on forage production and livestock weight gains in rangelands (Andales et al., 2005) and was applied for the semiarid rangeland systems in the region (Qi et al., 2012).

The GPFARM-Range model, using the Natural Resources Conservation Service (NRCS) recommended moderate SR, has been evaluated for forage production (Andales et al., 2005, 2006) and cow-calf weight gains (Andales et al., 2005), as well as soil carbon storage (Qi et al., 2012) in semiarid rangelands of North America. However, the model has not been evaluated for simulating long-term forage production and livestock weight gains for SR levels less than or greater than the moderate SR. Moreover, using the model to extend responses of forage production and livestock weight gains to SR greater than those previously experimentally evaluated can provide valuable information for land managers. For example, models could be used to determine the biophysical optimum SR for both forage production and livestock weight gains. To increase the value of GPFARM-Range model for land managers, the first objective of this study was to test the model for predicting forage production and livestock weight gains under three experimental SR treatments (low, moderate and high; see below) and long-term weather conditions on semiarid northern mixed-grass prairie in southeast Wyoming, USA. Our second objective was to quantify the threshold responses of forage production and livestock weight gains to SR and the yearly weather variability across years using long-term simulations with SR higher than those experimentally evaluated.

2. Materials and methods

2.1. Site description and field experiments

Experimental data used for model calibration and evaluation were from a long-term (31 yr) grazing experiment on semiarid northern mixed-grass prairie at the High Plains Grasslands Research Station (HPGRS) in Cheyenne, Wyoming, USA. (41°11'N, 104°53'W) (Hart et al., 1988; Manley et al., 1997; Derner and Hart, 2007; Derner et al., 2008b; Reeves et al., 2013b). Mean annual precipitation at the site is 381 mm with a peak in May and June. The soils are medium textured and well drained, dominated by

Albinas (fine-loamy, mixed, superactive, mesic pachic argiustolls) loam, with other soils including Altvan (fine-loamy over sandy or sandy-skeletal, mixed, superactive, mesic aridic argiustolls), and Ascalon (fine-loamy, mixed, superactive, mesic aridic agriustolls) loams (Stevenson et al., 1984).

Season-long (June–October), continuous grazing treatments were initiated in 1982 with three SR levels of low (8 steers/40 ha (0.2 steer ha⁻¹), about 35% below Natural Resources Conservation Service (NRCS)-recommended rate), moderate (8 steers/24 ha (0.33 steer ha⁻¹), the NRCS-recommended rate) and high (8 steers/18 ha (0.44 steer ha⁻¹), 33% greater than the NRCS-recommended rate; Hart et al., 1988). The moderate SR level (or similar) was most commonly practiced by the local ranchers in the region. Treatments were established using a randomized block design with two replicates (except for the low SR treatment without replicate) on a study area that had previously been grazed very lightly by livestock and wildlife (Hart et al., 1988). Yearling steers were used as grazing animals and each steer was weighed before and after the grazing season. All experimental procedures were performed according to HPGRS Animal Care and Use Committee oversight. Cattle did not graze pastures in 1989, 2000 and 2002 due to severe droughts. During the grazing period of 1982–2012, peak standing crop (PSC) was not measured in 2000 for the three SR treatments, and was measured starting in 1991 for the low SR treatment. Detailed information on the experiment can be found in Derner and Hart (2007), Derner et al. (2008b) and Reeves et al. (2013b).

2.2. Rangeland–Livestock model description and improvement

The forage and cattle modules of GPFARM are the simplified version of the Simulating Production and Utilization of Rangeland (SPUR) model (Hanson et al., 1988, 1992). The cattle module was modified to simulate steer herds with average steer forage consumption multiplied by the number of steers to estimate total herd consumption. Model specifications, including functions and equations for both the forage and cattle modules, have been published previously (Andales et al., 2005, 2006). The forage modules calculate daily forage growth and production, which are then used by the cattle modules to assess availability of forage and calculate daily forage intake and animal weight gain based on the demand for forage by animals. Subsequently, the forage modules are updated to incorporate grazing by the cattle module as described below.

In the original model, an index (massEffect) was used to restrict daily forage growth as influenced by grazing. The index for species *j* (massEffect_{*j*}) is calculated based on the following equation

$$\text{massEffect}_j = 1 - \frac{\text{netPrimProd}_j + \text{sForIntake}_j}{\text{speciesMax}_j} \quad (1)$$

where netPrimProd_{*j*} is net primary production for species *j* (kg ha⁻¹); speciesMax_{*j*} is the user-defined seasonal maximum forage production for species *j* (kg ha⁻¹); sForIntake_{*j*} is accumulated daily forage intake for forage species group *j* (kg ha⁻¹). The massEffect_{*j*} generally ranges from 1 (netPrimProd_{*j*} is 0 at the beginning of the season) to near 0 at the end of season. Because the difference in sForIntake_{*j*} between SR treatments is very small compared to the value of speciesMax_{*j*}, it has little influence on massEffect_{*j*} between SR treatments. Based on the Eq. (1) in the original model, less response (decrease) of PSC to the increased SR was simulated, compared to the observed PSC decrease from the low SR treatment (0.20 steer ha⁻¹) to the high SR treatment (0.44 steer ha⁻¹).

To improve the response of PSC to different SR treatments, an index of forage utilization (Eq. (2)), calculated from accumulated daily forage intake and total above ground biomass across the season according to previous studies (Whitson et al., 1976;

Rickert et al., 2000; Glindemann et al., 2009), was used to represent additional effects of different SR on forage growth and livestock weight gain

$$\text{Utilization}_j = \frac{s\text{ForIntake}_j}{\text{Forage}_j} \quad (2)$$

where $s\text{ForIntake}_j$ is defined in Eq. (1); Forage_j is the available forage from total above ground biomass for species j (kg ha^{-1}). The range of the index is from 0 at the beginning of grazing to 1 if all above ground biomass was grazed. Each forage species or functional group has its own utilization index.

The utilization index reflects grazing pressure, and showed close relationships with harvest efficiency or grazing efficiency as demonstrated by a previous study (Smart et al., 2010). It can be used to quantify the effect of SR on forage production, forage quality and diet digestibility, and cattle weight gain across various weather conditions. For example, the utilization index was used to quantify the effects of forage consumption by animals on subsequent forage growth by reducing the potential carbon fixation and transpiration and increasing soil evaporation due to reduction in leaf area (Rodriguez et al., 1990). It has been used to retard grass growth in a wheat grazing system model (Rodriguez et al. 1990) and to restrict the forage intake due to the decline in quality of diet as utilization increased (Rickert et al., 2000).

In this study, the index of Utilization_j was first used to describe the effect of grazing on PSC, and the massEffect_j calculation (Eq. (1)) was revised by adding the index of Utilization_j as follows

$$\text{massEffect}_j = 1 - \frac{\text{netPrimProd}_j}{\text{speciesMax}_j} \times (1 + \text{Utilization}_j) \quad (3)$$

If $\text{Utilization}_j = 0$ (no grazing), massEffect_j generally decreases from 1 (netPrimProd_j is 0 at the beginning of the season) to near 0 when netPrimProd_j is close to NetPrimProd_j at the end of season, which is same as Eq. (1). On the other hand, with the increase of Utilization_j , the massEffect_j will decrease and reduce the forage growth. If massEffect_j is lower than 0, then $\text{massEffect}_j = 0$.

The daily forage growth (ΔW_j , $\text{kg ha}^{-1} \text{d}^{-1}$) for species j is calculated from maximum growth rate (maxGrowthRate_j , $\text{kg ha}^{-1} \text{d}^{-1}$) and above ground biomass (AboveBio_j , kg ha^{-1}) for species j , and is reduced by environmental fitness factors (EVP, 0–1) and massEffect_j as shown in Eq. (4). The EVP includes temperature and water or nitrogen stress factors calculated by Eq. (5).

$$\Delta W_j = \text{maxGrowthRate}_j \times \text{AboveBio}_j \times \text{EVP} \times \text{massEffect}_j \quad (4)$$

$$\text{EVP} = \text{ETP} \times \min(\text{EWP}, \text{ENP}) \quad (5)$$

where ETP is effect of temperature on forage production (0–1) and EWP is effect of water availability on forage production (0–1). The ENP is effect of soil nitrogen stress on forage production (0–1). Hanson et al. (1988) discuss the empirical bases for the functions

in detail. The ETP function is an empirical bell-shaped curve with minimum (tempMinG), optimum (tempOptG), and maximum (tempMaxG) temperatures for growth. The EWP is a threshold-response curve that is a function of the ratio of actual evapotranspiration (ET) and potential ET, and water stress tolerance (waterStressTol). The ENP is an exponential function curve with forage shoot N content. Because native rangelands do not have commercial nitrogen fertilizer applied, they were presumed to have stable and low plant-available N levels. Thus, we did not calibrate the model for N stress, which is implicitly considered in the calibration of potential growth rate (maxGrowthRate_j ; Andales et al. 2005).

As the utilization index increases (Eq. (2)), the forage quality and diet digestibility will decrease, which will reduce the forage intake and livestock weight gain (Whitson et al., 1976; Glindemann et al., 2009; Rickert et al., 2000). The forage quality response to SR was described by modifying the current expression in GPFARM-Range model with a term involving the Utilization_j index:

$$\text{QualForage} = \sum_{j=1}^n \left(\text{forTDN}_j \times \text{relPref}_j \times \left(\frac{1}{\text{utilization}_j^2 + 1} \right) \right) \quad (6)$$

where QualForage is forage quality for all forage types (functional groups); forTDN_j is total digestible nutrients (TDN) for forage type j (0–1), which is related to the parameters of maximum TDN (forMaxTDN , kg kg^{-1}) and minimum TDN (forMinTDN , kg kg^{-1}) for forage type j ; relPref_j is the relative preference for forage type j (0–1), which is calculated as a function of cattle preference (foragePref) and relative amount of forage type j ; n is forage type number. We used utilization_j^2 instead of utilization_j based on observed differences in steer weight gain (SWG) between low and high SR treatments.

The parameter QualForage can influence total intake TDN (totIntakeTDN , $\text{kg TDN head}^{-1} \text{d}^{-1}$) and diet digestibility (Dig , 0–1), metabolic maintenance requirement (Maint , $\text{kg TDN head}^{-1} \text{d}^{-1}$) (Bourdon, 1983), and daily cattle weight gain (ΔCW , $\text{kg herd}^{-1} \text{d}^{-1}$) as follows

$$\text{totIntakeTDN} = \text{inSup} \times \text{QualSup} + \text{inForage} \times \text{QualForage} \quad (7)$$

$$\text{Dig} = \text{totIntakeTDN} / (\text{inSup} + \text{inForage}) \quad (8)$$

$$\text{Maint} = \frac{(0.077 \times +0.0052 \times (\text{weight} + \text{milkProd})^{0.75}}{3.6 \times (0.486 + 0.243 \times \text{Dig})} \quad (9)$$

$$\Delta \text{CW} = (\text{totIntakeTDN} - \text{Maint} \times \text{efficiency}) \quad (10)$$

where inSup and inForage are daily intake of supplement and forage (kg d^{-1}), respectively. QualSup and QualForage are the quality of supplement (0–1, depending on supplement type) and forage (0–1, calculated from Eq. (6)), respectively. The inForage is determined by animal weight (weight , kg herd^{-1}) and daily target weight gain (gain , $\text{kg herd}^{-1} \text{d}^{-1}$) and forage availability. The parameter of

Table 1

Statistics for observed and GPFARM-Range model simulated peak standing crop (PSC, kg ha^{-1}) and steer weight gain (SWG, kg head^{-1}) under the low (L, 0.20 steer ha^{-1}), moderate (M, 0.33 steer ha^{-1} , calibration) and high (H, 0.44 steer ha^{-1}) stocking rate treatments.

Treatments	Observed	Predicted from revised model			Predicted from original model		
	Mean $\pm$ SD	Mean $\pm$ SD	RMSE	Pair t -test	Mean $\pm$ SD	RMSE	Pair t -test
PSC							
L (Validation)	1578 $\pm$ 675	1351 $\pm$ 444	387	0.02	1376 $\pm$ 500	489	0.08
M (Calibration)	1279 $\pm$ 549	1204 $\pm$ 384	355	0.26	1353 $\pm$ 450	400	0.32
H (Validation)	1141 $\pm$ 464	1117 $\pm$ 386	358	0.76	1344 $\pm$ 453	425	0.005
SWG							
L (Validation)	111.4 $\pm$ 22.9	109.1 $\pm$ 14.8	14.2	0.26	110.8 $\pm$ 15.6	14.7	0.84
M (Calibration)	108.6 $\pm$ 21.2	103.2 $\pm$ 13.8	12.8	0.02	110.7 $\pm$ 15.6	12.8	0.38
H (Validation)	97.3 $\pm$ 22.1	94.6 $\pm$ 13.7	13.7	0.27	110.7 $\pm$ 15.6	21.1	0.0002

efficiency is feed utilization efficiency (0–1). Because no supplement was simulated in the current study ($\text{inSup} = 0$), Dig is equal to QualForage (Eqs. (7) and (8)). Maint will increase with increasing body weight and decreasing Dig (Eq. (9)), and cattle weight gain is determined by the difference between totIntake and Maint (Eq. (10)).

2.3. Model calibration and evaluations

Daily climate data for Cheyenne, Wyoming were taken from the National Atmospheric and Oceanic Administration (NOAA; <http://www.ncdc.noaa.gov/>). These included precipitation (mm), maximum and minimum air temperature ($^{\circ}\text{C}$), solar radiation (Langley day^{-1}), mean wind speed (m s^{-1}), and mean relative humidity (%). Soil properties of Albinas loam, as the dominant soil at the site, were obtained from the GPFARM soils database. Observed data as described in Section 2.1, including yearly PSC and monthly steer weight during grazing from 1982 to 2012 for moderate SR treatment were used for model calibrations. Observed data from the other two SR treatments (low and high SR treatments) were used

for model evaluations. The model was run continuously from 1982 to 2012 for the three SR treatments.

The parameter estimation software, PEST (Doherty, 2010), was used to optimize parameters in the model. One important restriction in PEST optimization is its sensitivity to local minima, the initial parameter values, and the given ranges of the parameters (Gupta et al., 2003). To cope with this, the initial forage growth parameters and cattle parameters were set according to previous studies at the site (Andales et al., 2005, 2006; Qi et al., 2012). According to the previous studies (Andales et al., 2005, 2006), the most sensitive parameters for PSC were maxGrowthRate , tempOptG , degree days to start of senescence (senGDD), and waterStressTol as shown in Eqs. (4) and (5). These parameters were calibrated by matching the simulated with observed yearly PSC from the moderate SR treatment (Appendix A). The cattle preference value for plant functional groups (foragePref) determines desirability as cattle forage, and can influence forage intake and utilization (Eq. (1)) and forage quality (QualForage) as shown in Eq. (4), which was also optimized with observed PSC and steer weight data (Table 1). Because the warm-season grasses and

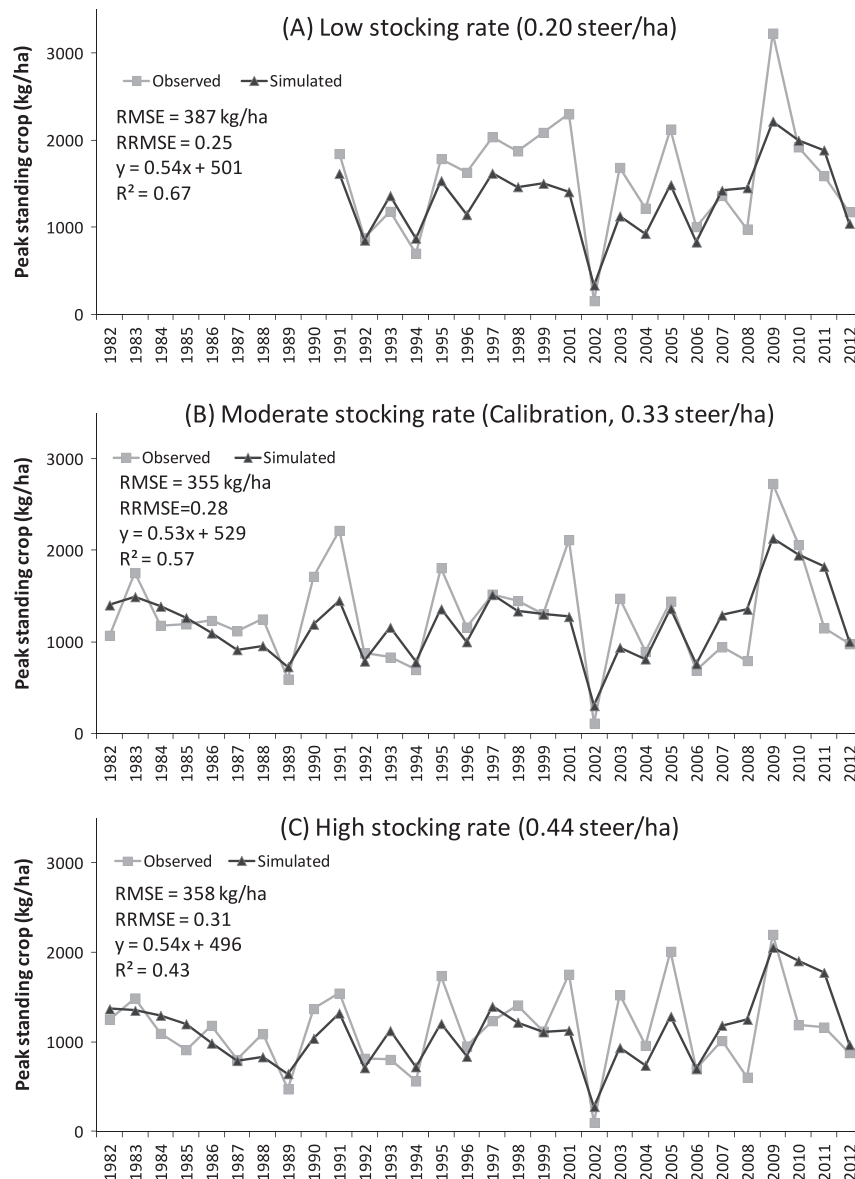


Fig. 1. Observed and GPFARM-Range model predicted peak standing crop from 1982 to 2012 under low (A), moderate (calibration, B), and high (C) stocking rate treatments.

cool-season grasses are the main functional groups in the northern mixed-grass prairie (Manley et al., 1997), above parameters were calibrated only for these two functional groups. The maximum forage production was set at 3250 kg ha⁻¹ according to the measured maximum PSC value of 3227 kg ha⁻¹ in 2009. Other forage parameters were set to their default values suggested in the model or from previous studies (Andales et al., 2005, 2006), and were not calibrated by PEST (Table 1). Other functional groups, such as shrubs and forbs, are rare and default parameters for them were used in the model according to previous study (Andales et al., 2006). Some animal parameters were from a previous study (Andales et al., 2005), such as animal feed requirement and mature weight. Other animal parameters of feed utilization efficiency (efficiency) and target weight gain (gain), influencing on the inForage and weight gain (Eqs. (7)–(10)), were calibrated based on the observed steer weight gain data (Table 1). Initial steer weight at the beginning of grazing was also input for each year based on the observed initial steer weight data before grazing.

To evaluate the model performance, the following statistics were used: root mean squared errors (RMSE; Eq. (11) below), relative RSME (RRMSE, Eq. (12) below) and coefficient of determination (R^2 , Eq. (13) below).

$$RMSE = \sqrt{\frac{\sum_{i=1}^n (O_i - P_i)^2}{n}} \quad (11)$$

$$RRMSE = \frac{RMSE}{O_{avg}} \quad (12)$$

$$R^2 = \left\{ \frac{\sum_{i=1}^n (O_i - O_{avg})(P_i - P_{avg})}{\left[\sum_{i=1}^n (O_i - O_{avg})^2 \right]^{0.5} \left[\sum_{i=1}^n (P_i - P_{avg})^2 \right]^{0.5}} \right\}^2 \quad (13)$$

where P_i is the i th predicted value, O_i is the i th observed value, P_{avg} and O_{avg} are the average of observed and simulated values, respectively, and n is the number of data pairs. A paired t test was used for statistical significance testing of the differences in observed and predicted PSC or SWG from 1982 to 2012 among the three SR treatments.

2.4. Long-term simulations with extended SR above the experiment levels and yearly variability analysis

Evaluating SR values greater than previously used experimental levels can determine if thresholds exist for influences of SR on forage production and livestock weight gains. Model simulations are needed for these determinations as constraints related to animal health and care protocols can be logistically problematic for experimental evaluations at very high SR. For this paper, following evaluation of the model with high SR, we assessed the forage production and livestock weight gains to SR that were 50% to 300% greater than the evaluated experimental high SR (0.44 steer ha⁻¹). We used 6 SR spanning this range: (1) 50% higher or 0.66 steer ha⁻¹, (2) 100% higher or 0.88 steer ha⁻¹, (3) 150% higher or 1.10 steer ha⁻¹, (4) 200% higher or 1.32 steer ha⁻¹, (5) 250% higher or 1.54 steer ha⁻¹, and (6) 300% higher or 1.76 steer ha⁻¹ to ascertain if a threshold existed for SR. Based on the long-term simulations, the yearly variability (risk) analysis was carried out for PSC, SWG and economic profit using statistic criteria of coefficient of variation (CV), skewness and the cumulative distribution functions (CDFs). Because the model did not simulate the carrying costs (such as supplement cost, salt, implants and transportation), a simple method was used to estimate the economic profit based on previous studies in the region (Hart et al., 1988; Manley et al., 1997). The purchase price in March and selling

price in October for the simulation period (1982–2012) were obtained from National Agricultural Statistics Service (NASS, http://www.nass.usda.gov/Statistics_by_Subject/Economics_and_Prices/index.asp). Initial steer weight and steer weight gain from the model simulations for these SR levels were used to estimate gross cost and income for each year. Because economic risk analysis was focused on the effect of SR on profits as influence by weather variability, costs of salt, implants, vaccination, trucking and other supplement were set as 30 US dollars per head for the year of 1985 according to Jose et al. (1985). The costs increased year by year due to the inflation in US (<http://usinfation.org/us-inflation-rate/>) and reached to 64 US dollars in 2012, which is similar to the current carrying cost.

3. Results and discussion

3.1. Model calibrations

The predicted PSC from our improved model showed similar trends as the observed data from 1982 to 2012 for the moderate

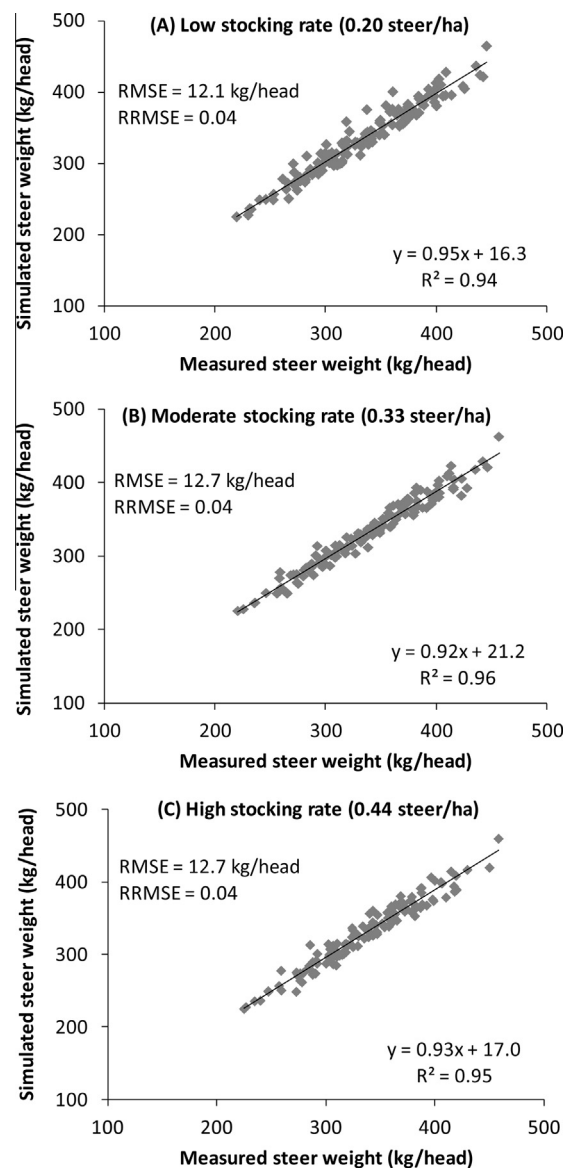


Fig. 2. Comparisons between observed and GPFARM-Range model predicted steer weight under low (A), moderate (B, calibration) and high (C) stocking rate treatments from 1982 to 2012.

SR (Fig. 1B), with a RMSE value of 355 kg ha^{-1} , and a RRMSE value of 0.28. These results were comparable or better than the previous study by Andales et al. (2006). Across the 30 years, the PSC was under-predicted by only 74.6 kg ha^{-1} and no significant difference was found between observed and simulated PSC based on a paired t -test ($P = 0.26$). The observed PSC showed a higher variation across years than predicted PSC (Table 1). The large error in predicted PSC in 2001 was likely due to the severe drought in 2000 (no observed data for 2000 due to the low forage production), especially since Andales et al. (2005) found that the model did not simulate the quick recovery of forage from severe drought.

Predicted steer weight gain (SWG, kg head^{-1}) was close to the observed data (Fig. 2B), with RMSE and RRMSE values of $12.7 \text{ kg head}^{-1}$ and 0.04, respectively. The model under-predicted SWG by 7.2 kg head^{-1} , which is consistent with the 74.7 kg ha^{-1} under-prediction of PSC. Predicted SWG showed similar trends with observed data from 1982 to 2012 (Fig. 3B), with RMSE value of $13.0 \text{ kg head}^{-1}$, and RRMSE value of 0.12. Some obvious

under-predictions of SWG were probably associated with under-predicted PSC (e.g., 1995 and 2001) or other predicted errors, such as in forage quality and diet digestibility (e.g., 1999, 2004, 2005 and 2007) (Fig. 3B). Averaged from 1982 to 2012, the predicted average yearly SWG was slightly lower by 5.4 kg head^{-1} (5.0%) than observed data (Table 1, “M” Treatment) that was consistent with the PSC under-predicted by 5.8%. A paired t -test showed significant difference between the observed and predicted data ($P = 0.02$), mainly likely due to the under-predictions of SWG in the above-mentioned years. As shown in Table 1, similar predictions of PSC and SWG for the calibrations (moderate SR treatment) were obtained from the original model, and the over-predicted SWG was consistent with the over-predicted PSC.

3.2. Model evaluations

Similar to the calibration results, predicted PSC from the revised model showed similar trends as the observed data from 1982 to

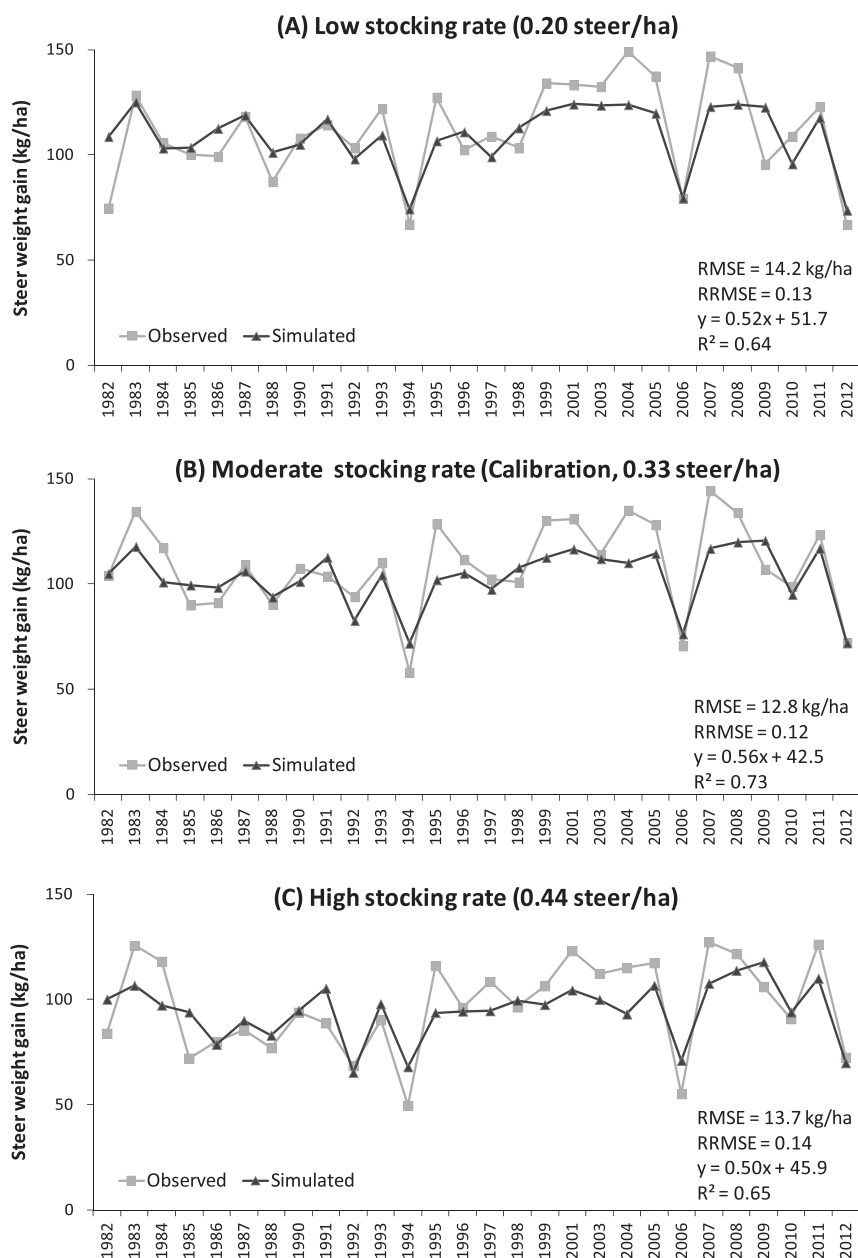


Fig. 3. Observed and GPFARM-Range model predicted yearly steer weight gain from 1982 to 2012 under low (A), moderate (calibration, B), and high (C) stocking rate treatments.

2012 for the low and high SR treatments (Fig. 1A and C). Average PSC was under-predicted by 227 kg ha^{-1} from 1991 to 2012 for low SR treatment, and by 24 kg ha^{-1} from 1982 to 2012 for high SR treatment (Table 1). There was no significant difference ($P=0.76$) between predicted and observed PSC from 1982 to 2012 for the high SR treatment based on a paired t -test, but a significant difference ($P=0.02$) between predicted and observed PSC for the low SR treatment.

The revised model predicted SWG was close to the observed data, with similar RMSE and RRMSE values (Fig. 2A and C). The within-season steer weight from 1982 to 2012 was slightly over-predicted by 0.9 kg head^{-1} for the low SR treatment, but was under-predicted by 6.7 kg head^{-1} for the high SR treatment (Fig. 2A and C). The predicted yearly SWG for the low and high SR treatments showed similar results compared to calibrations, with similar RMSE and RRMSE values (Fig. 3A and C vs. Fig. 3B). The paired t -test results showed no significant difference between predicted and observed yearly SWG for the low ($P=0.26$) and high ($P=0.27$) SR treatments.

We evaluated grazing effect differences between SR treatments (e.g., low vs. moderate (L-M); low vs. high (L-H); high vs. moderate (M-H)) for both observed and predicted data on yearly PSC and SWG. As shown in the x - y plane of observed difference vs. predicted difference (Fig. 4A), most of the data for PSC (97%) were in the 1st quadrant or near the origin of coordinate, indicating a good response to these SR treatments. Few data points, such as in 1991 and 2005, were in the 2nd quadrant due to the negative values of these observed differences for M-H or L-M. Most data in the 1st quadrant were below the 1:1 line especially when the observed differences were more than 400 kg ha^{-1} , suggesting under-predicted PSC difference by the model compared to the observed data. The high observed differences of 1000 kg ha^{-1}

(mean value is 437.8 kg ha^{-1}) between low and high SR treatments in 1999 and 2009 are attributable to the greater abundance of highly productive cool-season grasses (C_3 perennial grass) in the low compared to the high SR treatment (Derner et al., 2008a).

For the observed difference vs. predicted difference of yearly SWG (Fig. 4C), most of the data were in the 1st quadrant or near the origin of coordinate, and along the 1:1 line, except for some under-predicted differences for L-H and L-M. This result suggested that the model predicted well differences among treatments in terms of yearly SWG. The obvious negative value ($-29.3 \text{ kg head}^{-1}$) for observed difference in SWG in 1982 between light and moderate SR treatments was not simulated. Significant differences ($P < 0.001$) in yearly SWG was found between these SR treatments for both observed and predicted data based on the paired t -test.

The improved responses of the revised model (predicted PSC and SWG) to SR (Fig. 4A and C) were associated with the increased utilization index, decreased massEffect values, and reduced forage quality as SR increased (e.g., from 0.20 to 0.44 steer ha^{-1} as shown in Appendix B). In contrast, the original model showed significant difference from measured data for the high SR treatments ($P=0.005$ and 0.0002 , respectively) (Table 1). The corresponding RMSE values were also higher than for the revised model predictions (Table 1). The original model predicted the difference in PSC (Fig. 4B) or SWG (Fig. 4D) between these SR treatments to be nearly 0 or in the fourth quadrant, suggesting less response of predicted PSC or SWG to the increase of SR. On the other hand, significant difference ($P < 0.001$) in PSC (Fig. 4A) or SWG (Fig. 4C) between these SR treatments was found for both observed and the revised model predicted data based on the paired t -test.

The calibration and evaluation results showed that the revised model produced better PSC and SWG responses to different SR levels across seasons compared to the original model, and can be used

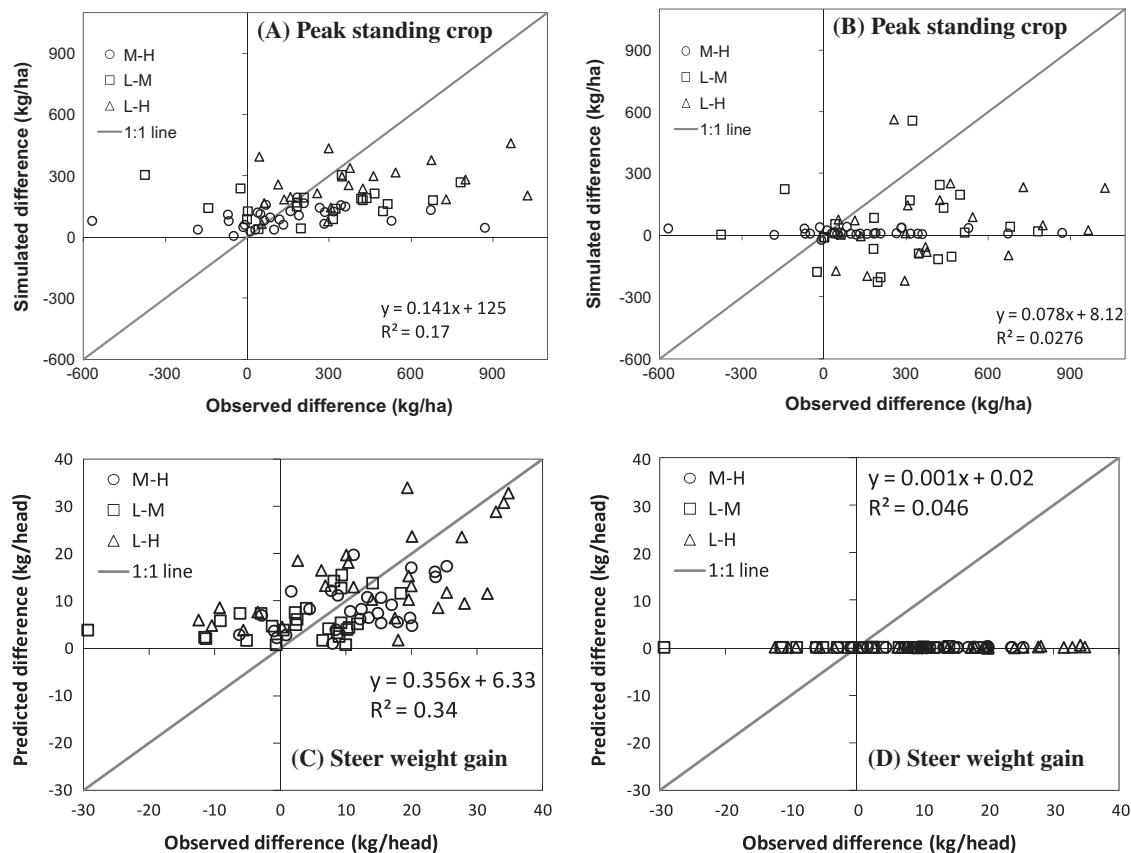


Fig. 4. Observed and predicted differences in peak standing crop or yearly steer weight gain per head among the low (L, $0.20 \text{ steer ha}^{-1}$), moderate (M, $0.33 \text{ steer ha}^{-1}$) and high (H, $0.44 \text{ steer ha}^{-1}$) stocking rate treatments from 1982 to 2012 by the revised (A and C) and original (B and D) GPFAARM-Range model.

to quantify the SR and seasonal weather variability effects on PSC and SWG.

3.3. Quantifying grazing and weather effects on PSC and SWG

3.3.1. Long-term SR effects on PSC and SWG and yearly variability

The predicted long-term (1982–2012) average PSC showed a decrease with increased SR ($PSC = 926.07SR^{-0.213}$, $R^2 = 0.99$; Fig. 5A), which was consistent with field experiment data. The predicted total forage intake (TotIntake, $kg\ ha^{-1}$, Fig. 5A) and total intake TDN (TotTDN, $kg\ TDN\ ha^{-1}$, Fig. 5B) increased quadratically with SR ($TotIntake = -208.65SR^2 + 1146.5SR - 56.09$, $R^2 = 1$; $TotTDN = -138.72SR^2 + 558.72SR + 2.45$, $R^2 = 1$; Fig. 5). The diminishing increase of TotIntake or TotTDN at high SR levels was mainly due to both decreased PSC (Fig. 5A) and forage quality as SR and Utilization index increased (Eqs. (2), (6), (7), and Appendix B). The simulated metabolic maintenance requirement per area (Maint, $kg\ TDN\ ha^{-1}$), however, increased linearly with increased SR ($Maint = 295.76SR + 1.52$, $R^2 = 1$; Fig. 5B), because the Maint per head (Eq. (9)) was relatively stable due to the decreased steer weight and diet digestibility with increased SR (Eqs. (6)–(8), and Appendix B). The quadratic response of SWG to SR showed a decline in the net return of SWG with the increase of SR, which was determined by the difference between TotTDN and Maint (Eq. (10)). The quadratic increase of TotTDN and linear increase of Maint resulted in quadratic increase of TotTDN-Maint as SR increased, where maximum TotTDN-Maint values at about 0.88 steer ha^{-1} produced maximum SWG (Fig. 5B).

As shown in Fig. 5C, the yearly variability (coefficient of variation, CV) in TotTDN-Maint increased exponentially from 0.21 to 3.81 as SR increased from 0.20 to 1.76 steer ha^{-1} , which was consistent with the increase of CV from 0.17 to 3.25 for SWG. The CV values for PSC (0.29–0.37), Maint (0.21–0.20) and TotTDN (0.18–0.28) changed less with SR compared to the CV change of SWG. This result indicated that the quadratic response of TotTDN and linear response of Maint to SR resulted in high yearly variability of SWG at high SR levels, which explained the higher sensitivity of SWG to seasonal weather variations under higher SR levels (Reeves et al., 2013b, 2014).

Fig. 5A and B showed threshold response of SWG per area to SR (about 0.88 steer ha^{-1}) and PSC (about 939 $kg\ ha^{-1}$) in the region. This biophysical optimum SR resulted in high harvest efficiency of 0.84 (total forage intake/PSC defined by Smart et al. (2010), Fig. 5A), and high yearly variability in SWG (CV values between 0.34 and 0.50) due to the weather variations (Fig. 5C). Recent field experimental studies have shown significant influence of spring rainfall amount (April–June) on PSC and SWG in the region, and can help ranchers make better SR decisions (Derner and Hart, 2007; Derner et al., 2008a; Wiles et al., 2011; Reeves et al. 2013a,b, 2014). We also found that the biophysical optimum SR with maximum SWG per area for each year from 1982 to 2012 showed a positive increase with spring rainfall ($SR = 0.0027Rainfall + 0.5346$, $R^2 = 0.24$, $P = 0.005$) or PSC ($SR = 0.0009PSC + 0.1743$, $R^2 = 0.51$, $P = 0.0001$).

The responses of PSC and SWG to SR under dry (below 80% average spring rainfall), normal (80–120% average spring rainfall), and wet (above 120% spring rainfall) weather conditions were further compared to select better SR for these different weather conditions (Fig. 6). As SR increased, the SWG per area increased more for the wet seasons than for the dry seasons due to the different PSC levels under the different weather conditions (Fig. 6). The biophysical optimum SR increased from about 0.88 steer ha^{-1} for the dry or normal seasons (Fig. 6A and B) to about 1.10 steer ha^{-1} for the wet seasons (Fig. 6C). The corresponding daily SWG per head was 0.36 $kg\ head^{-1}\ day^{-1}$ (dry seasons), 0.48 $kg\ head^{-1}\ day^{-1}$ (normal seasons), and 0.60 $kg\ head^{-1}\ day^{-1}$ (wet seasons), which

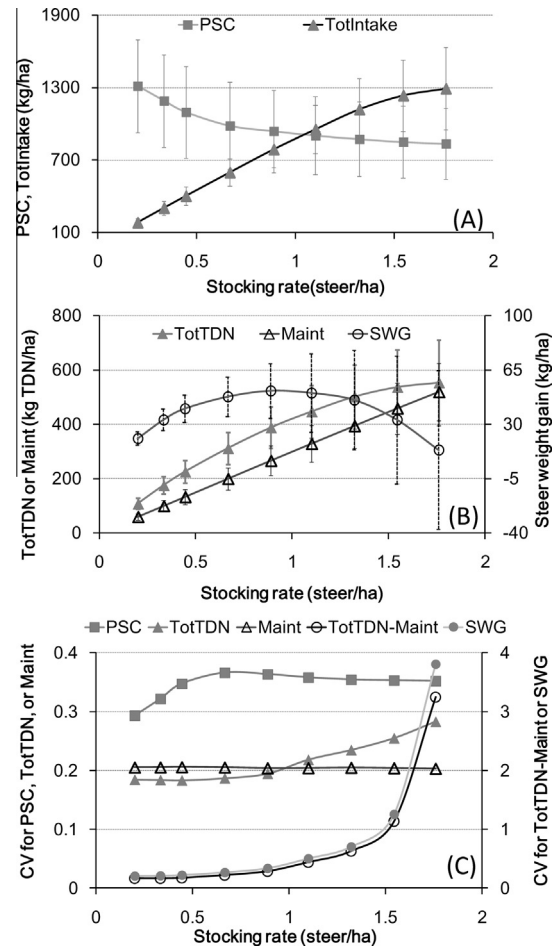


Fig. 5. GPFARM-Range model predicted long-term (1982–2012) average peak standing crop (PSC), total forage intake (TotIntake), total intake digestible nutrients (TotTDN), metabolic maintenance requirement (Maint) and steer weight gain (SWG), and the coefficient of variation (CV) for PSC, TotTDN, Maint, TotTDN-Maint and SWG across seasons as influenced by the stocking rates (SR) from 0.20 steer ha^{-1} to 1.76 steer ha^{-1} .

were much lower than the values reported for moderate SR (0.82 $kg\ head^{-1}\ day^{-1}$, Hart et al. 1988, and 0.83 $kg\ head^{-1}\ day^{-1}$ Manley et al. 1997).

Compared to the lowest SR of 0.20 steer ha^{-1} , the PSC at the biophysical optimum SR levels were reduced by 29%, 33% and 27%, with high harvest efficiency values of 0.98, 0.96 and 0.86 for the dry, normal and wet weather conditions, respectively (Fig. 6). The reduced PSC with increased harvest efficiency for the biophysical optimum SR likely affects ecosystem functions negatively, such as reducing soil carbon storage and increasing the risk of soil degradation as discussed by Derner and Hart (2007). The high yearly variability of SWG (CV = 0.47 for dry seasons; CV = 0.22 for normal seasons; CV = 0.33 for wet seasons) at these biophysical optimum SR levels also suggests elevated risks in obtaining these maximum SWG per area (Fig. 6). When considering the above results, the practical SR should be much lower than the biophysical optimum SR levels. Galt et al. (2000) proposed a harvest efficiency of 25% for moderate SR level, which can be obtained at SR levels between 0.22 and 0.33 steer ha^{-1} for the dry or normal weather seasons, or between 0.33 and 0.44 steer ha^{-1} for the wet weather seasons (Fig. 6). The above reduced SR levels resulted in higher marginal SWG, and can be more practical for ranchers to obtain high SWG per head and PSC with low yearly variability and avoid land degradations.

Based on the economic profits analysis (Fig. 6), the financially optimal SR with highest profits was considerably lower than the

biophysical optimum SR levels, and increased from about 0.33 steer ha⁻¹ for the dry seasons to about 0.44 steer ha⁻¹ for the wet seasons, with net returns increasing from \$13.19 ha⁻¹ to \$35.34 ha⁻¹. The low financially-optimum SR was mainly due to the faster rate of increase in cost relative to SWG, as SR increased (White and McGinty, 1997; Kemp et al., 2013). These financial optimum SR levels were 37.5%, 50%, and 40% of the biophysical optimum SR levels, for the dry, normal and wet seasons, respectively. Above results were close to the previous studies with experimental data in the region (Hart et al., 1988; Manley et al., 1997). The corresponding SWG per area was reduced by 32% (dry seasons), 20% (normal seasons) and 31% (wet seasons) from the SWG at biophysical optimum SR, respectively, but the yearly variability (CV) for SWG was reduced by 30% (dry seasons), 64% (normal seasons) and 75% (wet seasons) (Fig. 6). The average daily weight gain was 0.71 kg head⁻¹ day⁻¹ for dry season, 0.82 kg head⁻¹ day⁻¹ for normal season or 0.90 kg head⁻¹ day⁻¹ for wet season, with forage harvest efficiency of 0.32, 0.29 or 0.31, respectively. Such reduced SR levels can benefit the land ecosystem and may also produce higher quality products and possible higher economic profits as discussed by Kemp et al. (2013).

3.3.2. Seasonal PSC and SWG response to SR and risk analysis

The CDFs were developed as decision tools for evaluating the risks associated with different SR levels (Fig. 7). As SR increased, the simulated PSC at lower SR levels showed a first-degree stochastic dominance (FDSD) to the simulated PSC at higher SR level across these years (Fig. 7A). The CV and skewness values for the simulated PSC increased with SR from 0.20 to 0.88 steer ha⁻¹ and were stable at further higher SR levels (Table 2). The lowest SR resulted in both highest PSC and lowest yearly variability (lowest

CV). The Skewness values near zero (−0.08) for the simulated PSC at 0.20 steer ha⁻¹ indicated a normal distribution of PSC across these years. The higher skewness values for PSC at SR levels higher than 0.44 suggest a higher probability (risk) of obtaining lower PSC than average PSC across years.

The FDSD analysis for SWG per area (Fig. 7B) showed that the predicted SWG with higher SR unambiguously dominated the simulated SWG with lower SR when SR increased from 0.20 to 0.44 steer ha⁻¹. The predicted SWG with SR of 0.66 steer ha⁻¹ also dominated the predicted SWG with SR of 0.20 or 0.33 steer ha⁻¹, but showed higher yearly variability (CV) than the lower SR levels (Table 2). No other FDSD was found in the simulated SWG among these SR levels. As SR increased from 0.66 to 0.88 steer ha⁻¹, the predicted SWG increased but with higher yearly variability, and further increases in SR levels resulted in decreased predicted SWG with higher yearly variability (Table 2).

The CDFs for the net return from 1982 to 2012 showed an increase in economic profits with increased SR from 0.22 to 0.44 steer ha⁻¹ across most years (Fig. 7B). A decrease in profits occurred with increased SR levels of 0.44 or 0.88 steer ha⁻¹ and negative profits were obtained at SR levels between 1.10 and 1.76 steer ha⁻¹ due to reduced SWG and increased costs (Table 2). The high SR also resulted in high yearly variability of the profits compared with these lower SR levels between 0.22 and 0.44 steer ha⁻¹ (Table 2). The economic profits with SR level between 0.33 and 0.44 steer ha⁻¹ showed a second-degree stochastic dominance (SDSD) to the profits at SR between 0.66 and 0.88 steer ha⁻¹, which may be preferred by risk-averse ranchers.

These CDFs can help ranchers determine expected net return with a certain probability. For example, to obtain a higher PSC level than the 1218 kg ha⁻¹ for the moderate SR (Derner and Hart, 2007),

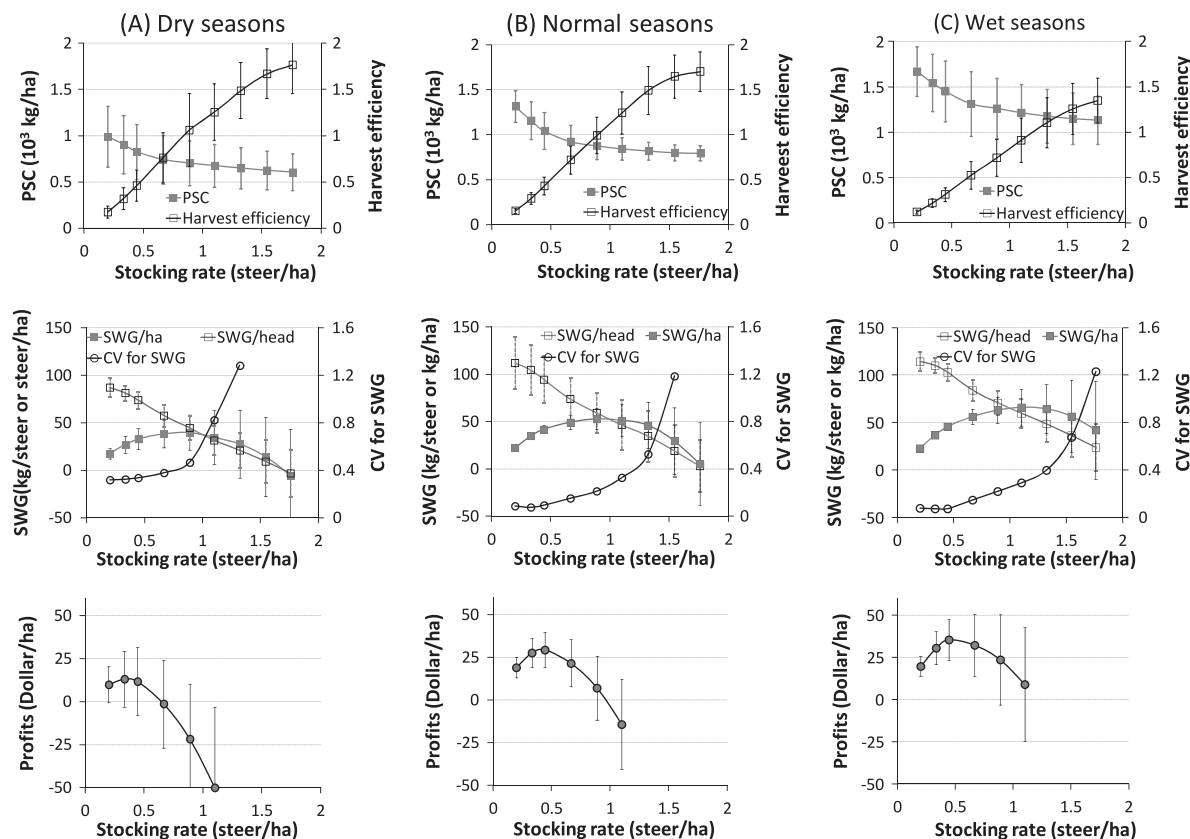


Fig. 6. GPFARM-Range model predicted long-term (1982–2012) average peak standing crop (PSC), harvest efficiency, steer weight gain (SWG) and economic profits for the dry seasons (spring rainfall (April–June) below 80% average level (135 mm), 11 seasons), normal seasons (spring rainfall between 80% and 120% average level (135–195 mm), 10 seasons), and wet seasons (spring rainfall above 120% average level (195 mm), 10 seasons) as influenced by stocking rate (SR) from 0.20 steer ha⁻¹ to 1.76 steer ha⁻¹. The coefficient of variation (CV) values for SWG and negative net return for the high SR are presented in Table 2.

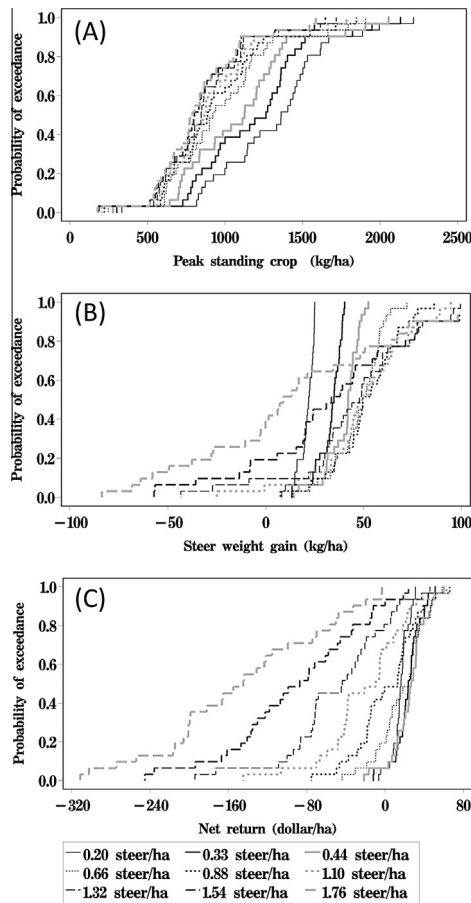


Fig. 7. Cumulative distribution functions of GPfARM-Range model predicted peak standing crop (PSC, kg ha⁻¹) (A) and yearly steer weight gain (B, kg ha⁻¹), and economic net return (dollar ha⁻¹) for the 9 stocking rates from 1982 to 2012.

a cumulative probability of 50% to 70% occurred for the 3 experimentally-evaluated treatments (L: 0.20 steer ha⁻¹; M: 0.33 steer ha⁻¹; H: 0.44 steer ha⁻¹), and a cumulative probability from 10% to 40% was found for SR > 0.44 steer ha⁻¹ (Fig. 7A). Similarly, SWG was below 50 kg ha⁻¹ 100% all years for the 3 experimentally-evaluated treatments (Fig. 7B), but resulted in positive profits at more than 90% of the time (Fig. 7C). Higher SR from 0.66 steer ha⁻¹ to 1.10 steer ha⁻¹ increased SWG to > 50 kg ha⁻¹ with a cumulative probability of about 50% of the time, but resulted in negative profits at 23% (SR = 0.66 steer ha⁻¹), 45% (SR = 0.88 steer ha⁻¹) and 68% (SR = 1.10 steer ha⁻¹) of the time. Further increases in SR decreased the probability (<50%) of obtaining higher than 50 kg ha⁻¹ SWG, and induced a probability above

80% of obtaining negative profits across the years. These results can help ranchers choose SR levels to lower risks of negative economic profits and rangeland degradation associated with yearly weather variations.

4. Conclusions and remarks

In the revised GPfARM-range model, grazing effects on forage growth and cattle weight gain were improved by incorporating an index of utilization based on previous studies. The improved model predicted the effects of SR on PSC and SWG adequately across years (root mean square errors from 355 to 387 kg ha⁻¹ for PSC and from 12.8 to 14.2 kg head⁻¹ for SWG), and can be used to predict forage production and cattle weight gain under different SR across various weather conditions on the northern mixed-grass prairie.

Long-term simulations extended the previous results on seasonal weather effects on PSC and SWG under experimental SR levels to coupled effects of seasonal weather variability and grazing management on PSC and SWG for a wider range of SR levels. The long-term simulation results showed that the biophysical optimum SR increased from 0.88 steer ha⁻¹ for the dry or normal seasons to 1.10 steer ha⁻¹ for the wet seasons, and the financial optimum SR increased from 0.33 steer ha⁻¹ for the dry or normal seasons to 0.44 steer ha⁻¹ for the wet seasons. The biophysical optimum SR produced the highest SWG (kg head⁻¹) with high yearly variability and resulted in low PSC with high harvest efficiency (possible land degradation), along with lower or negative economic profits. The financially optimum SR with relatively lower SWG per area produced highest economic profits with low yearly variability and higher PSC with lower harvest efficiency, and may benefit the stability of vegetation composition. At the financially optimum SR, higher SWG per head (daily SWG per head) occurred and resulted in an earlier date to reach selling weights. The CDFs risk analysis of the simulated PSC, SWG, and economic profits for these SR levels provide useful information for ranchers when selecting yearly SR, as they consider economic and environmental returns, as well as yearly variability associated with weather variations.

To further improve simulations of SWG by the GPfARM-range model, some additional variables could be included. One is the direct influence of weather variables and forage quality/quantity on SWG through changes in steer grazing behavior and energy use efficiency. For example, hot weather decreases steer grazing and forage intake (Trudell and White, 1981). The second is accounting for the effect of weather variables on both forage growth and forage quality (Craine et al., 2009). The under-predicted SWG in this study could be partly due to errors in predicted forage quality or diet digestibility, where cattle may have access to higher quality forage and result in high SWG in the field

Table 2
GPfARM-Range model simulated long-term (1982–2012) average peak standing crop (PSC, kg ha⁻¹), steer weight gain (SWG, kg ha⁻¹), economic profits (\$ ha⁻¹), and corresponding coefficient of variance (CV, standard deviation/average) and skewness across the years for the 9 stocking rate (SR) treatments.

Item	SR = 0.2	SR = 0.33	SR = 0.44	SR = 0.66	SR = 0.88	SR = 1.10	SR = 1.32	SR = 1.54	SR = 1.76
PSC									
Mean	1314	1192	1097	984	939	904	874	850	836
CV	0.29	0.32	0.35	0.37	0.36	0.36	0.35	0.35	0.35
Skewness	-0.08	0.28	0.52	0.76	0.81	0.82	0.81	0.78	0.72
SWG									
Mean	20.8	32.7	40	47.7	51.5	50.1	45.5	32.8	13.4
CV	0.21	0.21	0.22	0.27	0.34	0.5	0.71	1.26	3.81
Skewness	-1.47	-1.53	-1.38	-0.78	-0.37	-0.80	-0.80	-0.39	0.01
Profits									
Mean	16.0	23.5	25.1	16.9	2.2	-20.2	-49.0	-91.6	-144.7
CV	0.55	0.60	0.70	1.43	14.63	-2.19	-1.11	-0.76	-0.59
Skewness	-0.56	-0.64	-0.68	-0.58	-0.29	-0.64	-0.67	-0.36	-0.08

Appendix A1

Forage and cattle parameters used in the GPFARM-Range model calibrated using forage and cattle data from 1982 to 2012 under moderate stocking rate treatment (0.33 steer ha⁻¹).

Plant parameters	Definition	Warm season grasses		Cool season grasses	
		Final	Initial and range	Final	Initial and range
<i>Calibrated</i>					
foragePref	Forage preference by livestock	0.2	0.40 (0.2–0.55)	0.75	0.80 (0.7–0.9)
maxGrowthRate	Maximum relative growth rate	0.24	0.22 (0.20–0.26)	0.23	0.20 (0.18–0.24)
senGDD	Growing degree days until senescence begins	1600	1400 (1300–1700)	1000	1100(900–1300)
tempOptG	Optimum temperature for growth	31	30 (27–33)	18	20 (16–23)
waterStress	Water stress tolerance	0.18	0.20 (0.15–0.25)	0.15	0.15 (0.10–0.20)
propPop	Proportion of population from each functional group	0.39	–	0.53	–
<i>Default</i>					
matureGDD	GDDs to maturity	1500	–	2200	–
respRate	Respiration rate	0.03	–	0.03	–
tempMinG	Minimum temperature for growth	5	–	0	–
tempMaxG	Maximum temperature for growth	45	–	36	–
forMaxTDN	Maximum TDN in each functional group	0.64	–	0.67	–
forMinTDN	Minimum TDN in each functional group	0.54	–	0.57	–
Cattle parameters	Definition	Final	Initial and range		
Efficiency	Feed utilization efficiency	0.44	0.50 (0.40–0.60)		
Gain	Target weight gain	0.94	0.90 (0.75–0.95)		

“–”Indicates parameters without calibration which were taken from model default value or previous studies in the region (Andales et al., 2005).

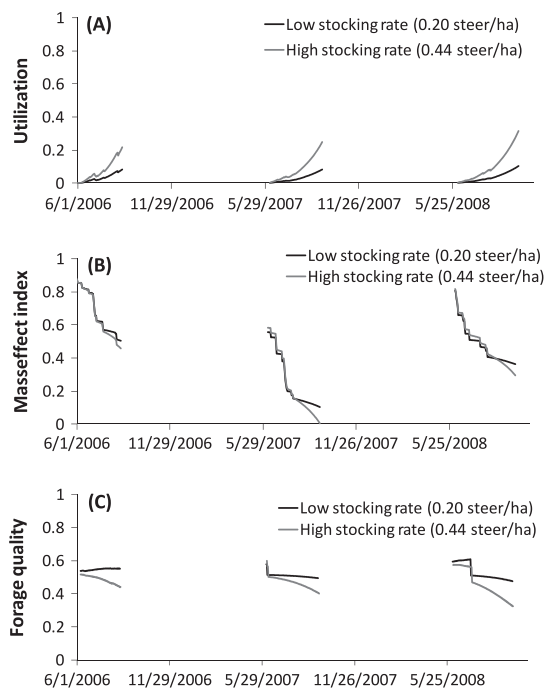
experiment. Inter-annual dynamics of the model merit improvement as the model did not capture carryover effects following a poor forage production year, nor the ability of this resilient rangeland ecosystem to recover from extreme weather (such as the 2000 drought).

Appendix A

See Appendix A1.

Appendix B

Comparisons of utilization index (Eq. (2), A), MassEffect index (Eq. (3), B) and forage quality index (Eq. (4), C) from 2006 to 2008 between low (0.20 steer ha⁻¹) and high (0.44 steer ha⁻¹) stocking rate treatments, as calculated by the improved GPFARM-Range model.

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