

Coupled Factors Influencing Concentration-Dependent Colloid Transport and Retention in Saturated Porous Media

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The coupled influence of input suspension concentration (C_i), ionic strength (IS), and hydrodynamics on the transport and retention of 1.1 μm carboxyl-modified latex colloids in saturated quartz sand (150 μm) under unfavorable attachment conditions (pH 10) was investigated. The percentage of retained colloids in column experiments decreased with C_i at intermediate IS conditions (31 or 56 mM) when colloids were weakly associated with the solid phase by a shallow secondary energy minima. In contrast, the effects of C_i on colloid retention were absent when IS was too low (6 mM) or too high (106 mM). The concentration effects under intermediate IS conditions were dependent on the system hydrodynamics, magnitude of C_i , and injection order of C_i , but they were largely independent of the input colloid mass. These observations were explained in part by time- and concentration-dependent filling of retention sites. Only a small fraction of the solid surface area was found to contribute to retention when IS was 31 mM, and micromodel observations indicated that colloid retention was enhanced in lower velocity regions of the pore space that occurred near grain–grain contacts. Consequently, retention profiles for IS = 31 mM conditions were increasingly nonexponential at lower values of C_i (during filling), whereas the observed concentration effect was largely eliminated as retention locations became filled. In addition, micromodel observations indicated that liquid and solid phase mass transfer of colloids to retention locations was influenced by C_i under intermediate IS conditions. Higher values of C_i are expected to produce less relative mass transfer to retention locations due to increased numbers of collisions that knock weakly associated colloids off the solid phase. Hence, the concentration effects were found to be largely independent of input colloid mass during filling of retention sites.

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Introduction

Aqueous concentrations of colloids vary widely in the environment as a result of differences in source as well as hydrologic, geochemical, and microbiological conditions (1–4). The potential influence of colloid concentration on the transport and fate of colloids in porous media has typically been neglected in studies that are designed to understand specific mechanisms of colloid retention. However, a limited number of studies have demonstrated that colloid concentration can have a large influence on the rates and mechanisms of colloid retention (5–12).

Results from previous studies regarding the effects of colloid concentration on retention have demonstrated a complex interplay between colloid concentration, pore size and geometry, colloid size, and aqueous phase velocity (9, 12). Furthermore, a variety of colloid retention mechanisms have been implicated in these studies that have time- and concentration-dependent behavior (10, 12). It is possible that the impact of colloid concentration is 2-fold, contributing to attachment and straining processes. Attachment involves collision with a solid–water interface and retention via adhesive forces. Time- and concentration-dependent attachment coefficients have been reported in the literature as a result of “blocking” or “ripening” (8, 13).

Straining processes involve colloid retention at or near multiple interfaces (14), and the potential for concentration effects is therefore dependent on the system geometry. When multiple colloids collide and are retained in a pore constriction, colloid retention has been reported to increase with increasing hydrodynamic forces and colloid concentration (9, 11) due to jamming and plugging of the pore constriction. In contrast, the colloid mass flux, pore space geometry, and system hydrodynamics are very different near grain–grain contacts (15). In particular, colloids that are weakly associated with the solid phase may be funneled by hydrodynamic forces toward these locations (15–17). In this case, increasing amounts of relative colloid (to the input concentration) retention have been observed with decreasing colloid concentration (12).

It should be mentioned that straining processes have traditionally been assumed to be purely a physical phenomena (17, 18) and, therefore, only determined by geometry considerations. Recent experimental evidence, however, indicates a strong coupling of straining processes on solution chemistry and hydrodynamics (19–22). The potential coupled influence of solution chemistry and colloid concentration on straining has not yet been reported in the literature. It is also possible that colloid aggregation may play a role in colloid retention at straining locations (23, 24), and this process is expected to be a function of hydrodynamics and the chemistry of the colloids and solution (14).

Although the above literature indicates that time- and concentration-dependent colloid transport and retention has previously been observed, our understanding of and ability to predict such behavior is limited because of the complex coupling of many relevant factors. The objective of this work is to investigate the coupled influence of colloid concentration with solution chemistry and hydrodynamics on retention mechanisms in packed bed column and micromodel experiments. Specific solution chemistry conditions are identified when concentration-dependent colloid transport is expected. Results from this work also have important implications for quantifying the evolution of the colloid retention profile over time, for determining the potential importance of transients

TABLE 1. Column Properties^a

| figure | IS (mM) | C_i (N_c mL ⁻¹) | q (cm min ⁻¹) | ϵ | L_c (cm) | T_o (PV) | M_{BTC} (%) |
|------------------|---------|----------------------------------|-----------------------------|------------|------------|------------------|-----------------|
| 1a | 6 | 3.6×10^6 | 0.09 | 0.37 | 13.2 | 1.4 | 93 |
| 1a | 6 | 3.6×10^9 | 0.10 | 0.37 | 13.2 | 1.5 | 91 |
| 1b | 31 | 3.6×10^6 | 0.12 | 0.41 | 13.6 | 1.6 | 5 |
| 1b | 31 | 3.6×10^7 | 0.12 | 0.41 | 13.7 | 1.6 | 3 |
| 1b | 31 | 3.6×10^8 | 0.14 | 0.39 | 13.1 | 2.0 | 67 |
| 1b | 31 | 3.6×10^9 | 0.12 | 0.36 | 12.5 | 2.1 | 92 |
| 2a | 31 | 3.6×10^6 | 0.56 | 0.36 | 13.0 | 1.8 | 33 |
| 2a | 31 | 3.6×10^9 | 0.57 | 0.36 | 13.1 | 1.8 | 78 |
| S3 ^b | 31 | 3.6×10^7 | 0.25 | 0.37 | 13.3 | 19.3 | 32 |
| S3 ^b | 31 | 3.6×10^8 | 0.25 | 0.37 | 13.1 | 1.9 | 85 |
| 1c | 56 | 3.6×10^6 | 0.12 | 0.41 | 13.6 | 1.6 | 6 |
| 1c | 56 | 3.6×10^7 | 0.11 | 0.41 | 13.7 | 1.4 | 2 |
| 1c | 56 | 3.6×10^8 | 0.11 | 0.39 | 13.1 | 1.7 | 3 |
| 1c | 56 | 3.6×10^9 | 0.10 | 0.36 | 12.5 | 1.7 | 31 |
| 2b | 56 | 3.6×10^6 | 0.56 | 0.37 | 13.3 | 1.7 | 7 |
| 2b | 56 | 3.6×10^9 | 0.61 | 0.35 | 12.9 | 2.0 | 42 |
| 1d | 106 | 3.6×10^6 | 0.10 | 0.37 | 13.2 | 1.5 | 0 |
| 1d | 106 | 3.6×10^9 | 0.09 | 0.36 | 13.0 | 1.5 | 0 |
| 4 | 31 | MP1 ^c | 0.52 | 0.36 | 12.9 | PV1 ^d | 52, 81, 85, 112 |
| S3a ^b | 31 | MP2 ^e | 0.26 | 0.37 | 13.3 | 1.9 | 38, 65 |
| S3b ^b | 31 | MP3 ^f | 0.25 | 0.36 | 13.1 | 1.9 | 58, 39, 88, 105 |

^a Properties include porosity, ϵ ; column length, L_c ; Darcy velocity, q ; pulse duration, T_o , in terms of pore volume, PV , and percent recovery in the BTC (M_{BTC}) for each experimental system. ^b Figure is in the Supporting Information. ^c MP1 = C_i pulses of 3.6×10^7 , 3.6×10^9 , 3.6×10^8 , and 3.6×10^7 N_c mL⁻¹. ^d PV1 = 1.7, 1.3, 3.4, and 2.5 PV. ^e MP2 = C_i pulses of 3.6×10^6 , 3.6×10^8 N_c mL⁻¹. ^f MP3 = C_i pulses of 3.6×10^8 , 3.6×10^7 , 3.6×10^9 , 3.6×10^7 N_c mL⁻¹.

in suspension concentration on colloid fate, and for predicting long-term colloid transport.

Materials and Methods

Experiments used aqueous solutions of NaCl for the eluting and resident solutions and NaBr for the tracer solution. To achieve highly unfavorable attachment conditions, we used solutions consisting of deionized (DI) water with its pH adjusted to 10 using 1.7 mM of Na₂CO₃ and 1.7 mM of NaHCO₃. Four ionic strength (IS) levels were considered in the experiments: 6, 31, 56, and 106 mM.

Fluorescent (excitation at 505 nm, emission at 515 nm) carboxyl-modified latex (CML) microspheres (Molecular Probes, Eugene, OR) were used in the colloid studies. The microspheres are reported by the manufacturer to be 1.1 μ m in size and hydrophilic, with a density of 1.05 g cm⁻³. The uniformity of the colloid size was verified using a Horiba LA 930 (Horiba Instruments, Inc., Irvine, CA) laser scattering particle size and distribution analyzer. The zeta potential of these microspheres in the various solution chemistries was calculated from experimentally measured electrophoretic mobilities using a ZetaPALS instrument (Brookhaven Instruments Corporation, Holtsville, NY) and the Smoluchowski equation. Colloid suspension input concentrations (C_i) used in experiments (Table 1) ranged over 3 orders of magnitude (from 3.6×10^6 to 3.6×10^9 N_c mL⁻¹, where N_c is the number of colloids). Average (three measurements) colloid concentrations reported herein were determined using a Turner Quantech fluorometer (Barnstead/ThermoLynce, Dubuque, IA), and reproducibility was typically within 1% of C_i .

Ottawa sand was employed in transport and batch studies. Ottawa sand, which is a natural aquifer material reported to consist of 99.8% SiO₂ (quartz) and trace amounts of metal oxides, is spheroidal in shape with a rough surface. Quartz and iron oxides possess a net negative charge at pH 10, and any attractive electrostatic interactions between the colloids

and porous medium are expected to be minimized at this pH. The median grain size of the sand was 150 μ m, and the coefficient of uniformity was 2.25. The zeta potential of these sands under the various solution chemistry conditions was estimated from literature values measured for quartz sand (25, 26).

The total interaction energy of the 1.1 μ m CML colloids upon approach to a quartz surface under various solution chemistries (pH 10, IS = 6, 31, 56, and 106 mM) was calculated using the Derjaguin–Landau–Verwey–Overbeek (DLVO) theory and a sphere–plate assumption (27, 28). Electrostatic double layer interactions were quantified using the expression of Hogg et al. (29) using zeta potentials in place of surface potentials. The retarded London–van der Waals attractive interaction force was determined from the expression of Gregory (30) utilizing a value of 4.04×10^{-21} J for the Hamaker constant (31).

Batch experiments were conducted by placing 10 g of sand and 10 mL of a colloid suspension with a known C_i (3.6×10^6 or 3.6×10^9 N_c mL⁻¹) and IS into a 20 mL glass scintillation vial. The suspension and sand were allowed to equilibrate for 4 h at 8 rpm using an orbital shaker (Lab-Line, Melrose Park, IL), and the final colloid concentration (C_f) was measured. All batch experiments were replicated, and blanks were run to determine the background interference from the sand. The retention of colloids in the batch system (R_B) was determined as $1 - (C_f/C_i)$.

Procedures and protocols for obtaining the breakthrough curves (BTCs) and retention profiles (RPs) in the saturated packed column (15 cm long and 4.8 cm inside diameter) experiments are reported in detail by Bradford et al. (20, 32) and are in the Supporting Information. Table 1 provides values of porosity (ϵ), column length (L_c), Darcy velocity (q), colloid pulse duration (T_o) in terms of pore volume (PV), and the percent recovery of injected colloids in the breakthrough curve (M_{BTC}) for each experiment. Most of the transport experiments were replicated, and this information is summarized in Table S1 of the Supporting Information. Replicate experiments conducted with the same batch of colloids exhibited very good reproducibility as demonstrated in Figure S1 of the Supporting Information. Differences in the replicate column experiments were more pronounced when using a new batch of colloids, presumably due to slight variations in colloid properties. To overcome this limitation, we based the figures and data comparison presented in this manuscript on a given batch of colloids.

An additional transport experiment was conducted in a specially designed micromodel to microscopically examine the retention behavior of colloids in the sand. Details on the experimental micromodel procedures are given in Bradford et al. (33) and in the Supporting Information.

Results and Discussion

Table 2 presents values for the zeta potential of the sand and colloids under the various experimental conditions considered in this work. DLVO calculations were conducted using this information, and the predicted height of the energy barrier (Φ_{max}) to deposition in the primary minimum and the depth of the secondary minima (Φ_{2min}) are also presented in Table 2. The value of Φ_{max} is $>1154 k_B T_K$ (where k_B is the Boltzmann constant and T_K is the absolute temperature) in all cases, indicating unfavorable conditions for attachment in the primary minimum. The magnitude of Φ_{2min} increases with increasing IS due to compression of the diffuse double layer thickness.

Results from batch experiments using sand and colloids at $C_i = 3.6 \times 10^9$ N_c mL⁻¹ and IS = 6, 31, 56, and 106 mM are given in Table 2. The background interference from the sand was very minor ($<2\%$ of C_i), and R_B of replicate

TABLE 2. Total Interaction Energy Parameters for 1.1 μm CML Colloids as a Function of IS^a

| IS (mM) | ζ_c (mV) | ζ_s (mV) | Φ_{max} ($k_B T_K$) | $\Phi_{2\text{min}}$ ($k_B T_K$) | R_B (%) |
|---------|----------------|----------------|-----------------------------------|------------------------------------|-----------|
| 6 | -107 | -80 | 5824 | -0.2 | 5 |
| 31 | -91 | -54 | 2709 | -1.3 | 7 |
| 56 | -96 | -53 | 2608 | -2.3 | 18 |
| 106 | -44 | -52 | 1154 | -5.0 | 27 |

^a The energy barrier height (Φ_{max}) and the depth of the secondary energy minima ($\Phi_{2\text{min}}$) were obtained from DLVO calculations using zeta potentials for colloids (ζ_c) that were measured and for sand grains (ζ_s) that were estimated from the literature (25, 26). The average batch colloid retention (R_B) is also present at an initial colloid concentration of $3.6 \times 10^9 N_c \text{ mL}^{-1}$ for the various IS.

experiments varied <7% of C_i . The average value of R_B was low (5%) in the 6 mM system that was associated with a very shallow $\Phi_{2\text{min}}$ ($-0.2 k_B T_K$), suggesting that minimal colloid attachment occurred in the primary minimum as a result of chemical heterogeneity. Conversely, the average value of R_B increased with IS due to a greater magnitude of the $\Phi_{2\text{min}}$ (<27%). This suggests the potential for limited association of colloids in the $\Phi_{2\text{min}}$ (note that Φ_{max} was very high). Similar trends were observed from running replicate batch experiments at the lower C_i of $3.6 \times 10^6 N_c \text{ mL}^{-1}$, with average values of R_B ranging from 9% to 29%. Hence, batch results were consistent with the DLVO calculations shown in Table 2 and demonstrate the existence of unfavorable attachment conditions.

Panels a–d of Figure 1 present representative colloid BTCs when q was approximately 0.1 cm min^{-1} and IS was 6, 31, 56, and 106 mM, respectively. Here, relative effluent concentrations (C/C_i) are plotted as a function of PV. Colloid retention increases with IS for a given value of C_i . This trend is expected (15), and is related to the increase in the depth of $\Phi_{2\text{min}}$ (Table 2). To study the influence of C_i on transport and retention, we conducted these experiments using C_i over a wide range (3.6×10^6 and $3.6 \times 10^9 N_c \text{ mL}^{-1}$). It was observed that varying C_i over 3 orders of magnitude did not have much of an effect on the BTCs when the IS was 6 (Figure 1a) or 106 mM (Figure 1d). In contrast, the BTCs were dependent on C_i when the IS was 56 mM and especially sensitive when the IS was 31 mM. Additional transport experiments were therefore conducted using intermediate values of C_i equal to 3.6×10^7 and $3.6 \times 10^8 N_c \text{ mL}^{-1}$ when the IS was 31 and 56 mM, respectively. Under these conditions, lower values of C/C_i were observed with decreasing C_i . When the IS was 31 mM, the value of M_{BTC} varied from 5% at $C_i = 3.6 \times 10^6 N_c \text{ mL}^{-1}$ to 92% at $C_i = 3.6 \times 10^9 N_c \text{ mL}^{-1}$ (Table 1). Similar trends were observed in replicate experiments summarized in Table S1 of the Supporting Information. These observations demonstrate a coupled effect of IS and C_i on colloid retention, which may be explained as follows. The magnitude of $\Phi_{2\text{min}}$ and the fraction of colloids that interact with the solid phase increase with IS (Table 2). Little colloid interaction with the solid phase occurred when the IS was 6 mM, and no influence of C_i on retention was therefore observed. When colloids are weakly associated with the solid phase in a shallow $\Phi_{2\text{min}}$ (IS = 31 mM and 56 mM), we hypothesize that they are susceptible to removal via colloid collisions (especially when IS = 31 mM), which increase in frequency with C_i and therefore produce less retention. In contrast, when IS was 106 mM, no effect of C_i was observed because the depth of the $\Phi_{2\text{min}}$ is greater and it is more difficult for collisions to remove colloids from the solid.

Additional column experiments were conducted to better understand the effect of C_i on colloid transport and retention. The influence of hydrodynamics was investigated by running

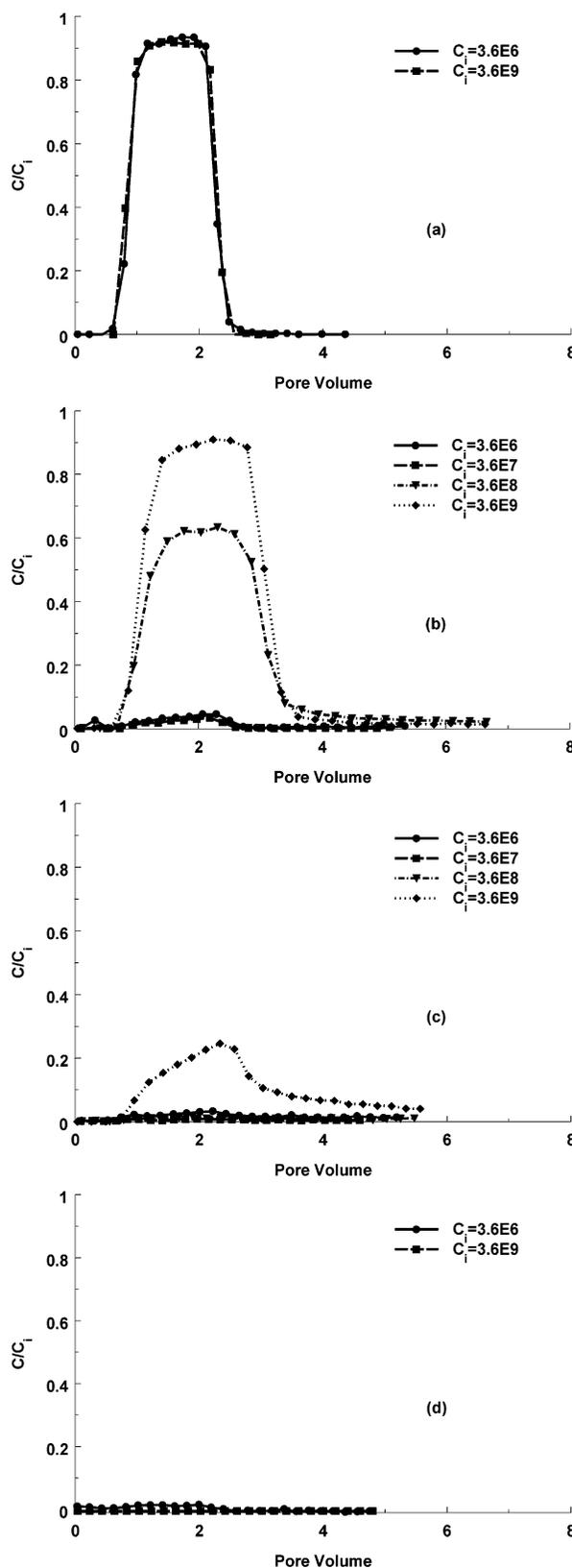


FIGURE 1. Breakthrough curves for 1.1 μm CML colloids in 150 μm Ottawa sand when $q \approx 0.1 \text{ cm min}^{-1}$, pH 10, and IS = 6 (a), 31 (b), 56 (c), and 106 (d) mM. A wide range of C_i values were considered in these experiments, and specific values are indicated in the legend.

similar experiments to those shown in Figure 1 but at a velocity 5 times higher. Panels a and b of Figure 2 present representative colloid BTCs when q was approximately 0.5 cm min^{-1} and IS was 31 and 56 mM, respectively. The value

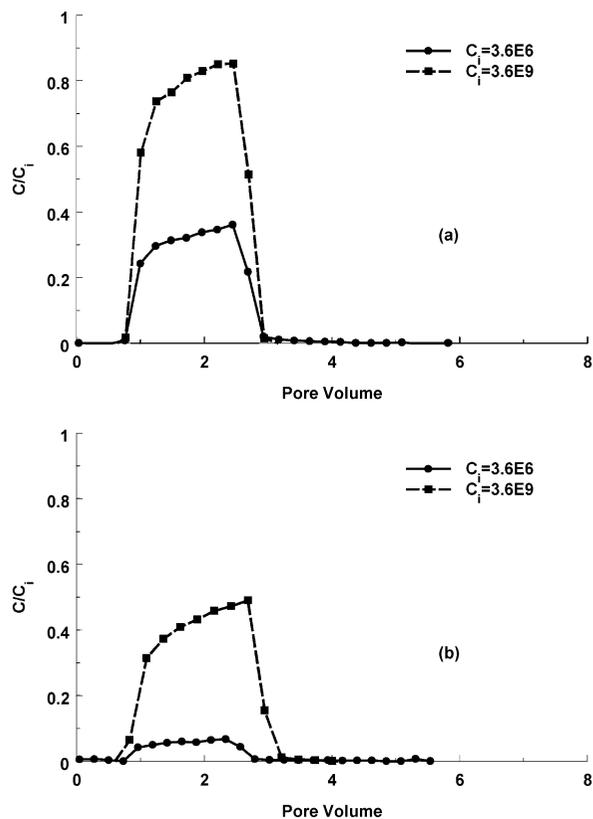


FIGURE 2. Breakthrough curves for $1.1 \mu\text{m}$ CML colloids in $150 \mu\text{m}$ Ottawa sand when $q \approx 0.5 \text{ cm min}^{-1}$, pH 10, and IS = 31 (a) and 56 (b) mM. A wide range of C_i values were considered in these experiments, and specific values are indicated in the legend.

of C_i was varied over 3 orders of magnitude (3.6×10^6 and $3.6 \times 10^9 N_c \text{ mL}^{-1}$), and the BTCs showed a similar sensitivity to C_i as shown in panels b and c of Figure 1, with decreasing C_i resulting in lower peak values of C/C_i . Comparison of panels b and c of Figure 1 and panels a and b of Figure 2 at similar IS and C_i conditions and the corresponding value of M_{BTC} (Table 1 and Table S1 of the Supporting Information) indicates that the effect of C_i on colloid retention is also a function of the system hydrodynamics. Several plausible explanations for the coupled effect of q and C_i include the following. The kinetic energy of colloid collisions increases with the square of the particle trajectory velocity. Velocity will also influence the forces and torques that act on colloids near solid surfaces, with higher velocities leading to a smaller fraction of the solid surface that contributes to retention (21). Hence, an increase in velocity is expected to decrease colloid retention at a given C_i . This indeed occurs for systems with the greatest amount of relative retention; i.e., for the IS = 56 mM system at both C_i values and for IS = 31 mM system at $C_i = 3.6 \times 10^6 N_c \text{ mL}^{-1}$ (Table 1 and Table S1 of the Supporting Information). Consequently, the difference in the M_{BTC} at $C_i = 3.6 \times 10^6$ and $3.6 \times 10^9 N_c \text{ mL}^{-1}$ for the IS = 56 mM system is greater when q is highest (Figures 1c and 2b, Table 1, and Table S1 of the Supporting Information). In contrast, decreasing retention at a higher q in the $C_i = 3.6 \times 10^6 N_c \text{ mL}^{-1}$ and IS = 31 mM system reduces the difference in the M_{BTC} at the two C_i extremes because of relatively minor amounts of retention at the highest C_i .

A micromodel experiment was conducted to better identify locations of colloid retention and mechanisms of mass transfer under conditions when C_i had a large influence on colloid retention. These experiments mimicked conditions used in Figure 1b (IS = 31 mM) with $C_i = 3.6 \times 10^9 N_c \text{ mL}^{-1}$. Figure 3 presents illustrative images of retained colloids in

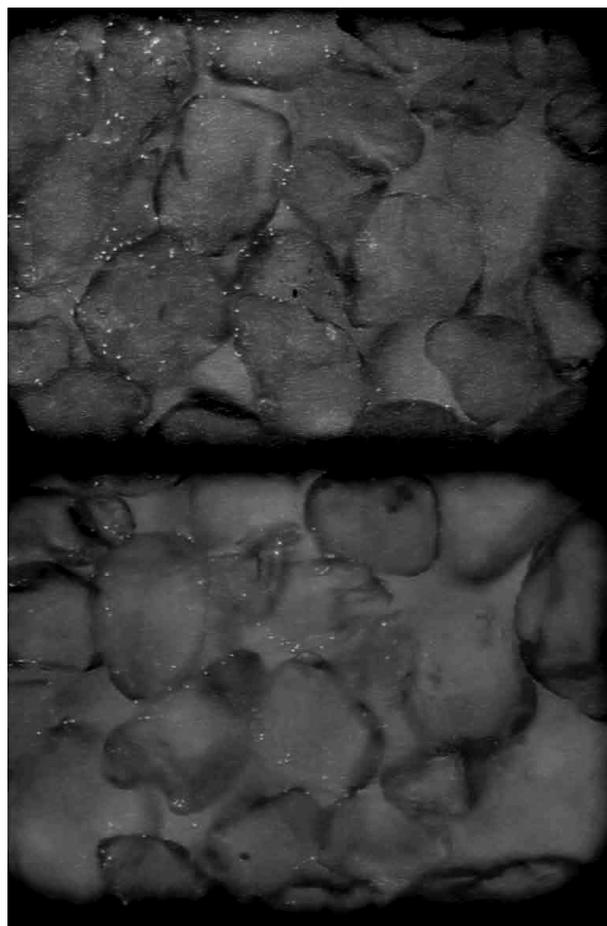


FIGURE 3. Illustrative microscopic images of retained $1.1 \mu\text{m}$ CML colloids in $150 \mu\text{m}$ Ottawa sand after recovery of the breakthrough curve; $q \approx 0.1 \text{ cm min}^{-1}$, pH 10, IS = 31 mM.

sand after recovery of the BTC. It was observed that colloid retention occurred primarily near grain–grain contact points that are associated with low velocities (15). Torque balance calculations presented by Torkzaban et al. (15) indicate that such locations are hydrodynamically favorable for colloid retention. Visual observations confirmed that mass transfer to these locations occurred by low advective and dispersive fluxes in the aqueous phase as well as along the solid phase. Only limited colloid retention was observed away from grain–grain contacts. Figure S2a of the Supporting Information and the associated discussion further substantiate these findings. Published fluorescent microscopy and X-ray microtomography studies have also demonstrated that colloids accumulate in narrow regions of pore spaces near the contacts of irregularly shaped sand grains (23, 24, 33–37) and may be translated on the solid surface in the presence of fluid drag (38) and a weak $\Phi_{2\text{min}}$.

Additional experiments were conducted to study the influence of temporal changes in C_i on colloid retention. Figure 4 presents multipulse colloid BTCs with different step inputs of C_i indicated in the legend. These experiments were conducted when q was 0.5 cm min^{-1} and IS was 31 mM. When the input pulse of C_i was increased from 3.6×10^7 to $3.6 \times 10^9 N_c \text{ mL}^{-1}$, a similar concentration effect was observed in C/C_i as was found in Figure 1b (increasing C_i resulted in a higher value of C/C_i). Conversely, when the input pulse of C_i was subsequently decreased from 3.6×10^9 to 3.6×10^8 to $3.6 \times 10^7 N_c \text{ mL}^{-1}$, the concentration effect was largely eliminated, and values of C/C_i slowly approached a value of 0.95. In this case, the BTCs were slightly affected by background concentrations from higher C_i pulses, and this influenced the concentration tailing

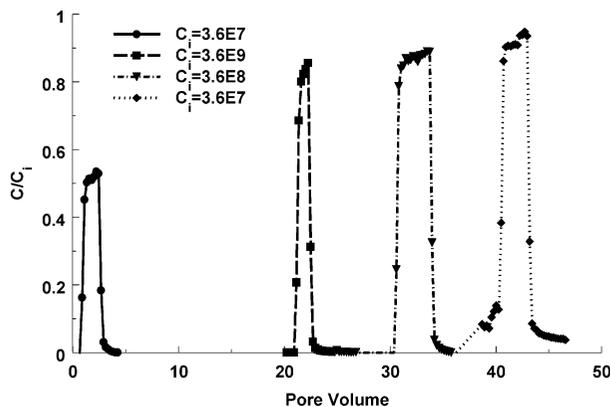


FIGURE 4. Multiple pulse breakthrough curves with different step inputs of C_i indicated in the legend. These experiments were conducted using $1.1 \mu\text{m}$ CML colloids in $150 \mu\text{m}$ Ottawa sand; $q \approx 0.5 \text{ cm min}^{-1}$, pH 10, and IS = 31 mM.

behavior (<14% of C/C_i). Figure S3 of the Supporting Information provides additional transport data that show similar trends during transients in C_i at a different velocity. These observations indicate that as hydrodynamically favorable retention locations such as near grain–grain contacts become filled the concentration effect tended to disappear. This is analogous to chemically favorable sites being saturated. It implies a maximum cover of colloid retention under given system conditions (pore space geometry, hydrodynamics, and chemistry), which is independent of C_i . It should be noted that higher C_i will fill retention sites more rapidly than lower C_i .

To better understand the influence of C_i on the filling of retention sites, we need to examine the RPs. Figure 5 presents the RPs when q was approximately 0.1 cm min^{-1} , IS was 31 mM, and C_i was 3.6×10^6 , 3.6×10^7 , 3.6×10^8 , and $3.6 \times 10^9 \text{ N}_c \text{ mL}^{-1}$. The corresponding BTCs for these systems were presented earlier in Figure 1b. Good mass balance was achieved in these experiments (90–103%). This suggests minimal errors were associated with our experimental protocols, and limited amounts of colloid attachment occurred in the primary minimum. In Figure 5a, relative concentrations ($N_c N_{ic}^{-1} \text{ g}^{-1}$, where N_{ic} is the number of colloids in a unit volume of C_i) of retained colloids are plotted as a function of depth from the column inlet. In Figure 5b, the absolute concentration of retained colloids ($N_c \text{ g}^{-1}$) is plotted on a semilog scale as a function of depth to easily tell if the data is consistent with a first-order deposition model (log–linear). The shape of the RP in Figure 5 was highly dependent on C_i . Lower values of C_i produced nonexponential profiles (Figure 5b) and greater relative amounts of retention near the column inlet (Figure 5a). Conversely, higher values of C_i produced nearly exponential RP and higher amounts of absolute retention (Figure 5b and Figure S2b of the Supporting Information). These observations suggest a fixed number of retention locations, that the rate of filling of these sites was a function of C_i , and that the RPs were nonexponential with depth until the retention locations filled. Note, however, that colloid heterogeneity cannot explain the nonexponential RPs in Figure 5 because the only difference in the colloidal suspensions was due to concentration. Alternatively, one plausible explanation for this behavior is enhanced rates of colloid retention in low velocity regions (39) as was confirmed by micromodel observations. Additional discussion pertaining to the rather unusual shape of the RP for the $C_i = 3.6 \times 10^8 \text{ N}_c \text{ mL}^{-1}$ system in Figure 5 is provided in Figure S2b and the text of the Supporting Information.

The fraction of the sand surface area (S_f) that contributed to colloid retention may be determined from the maximum

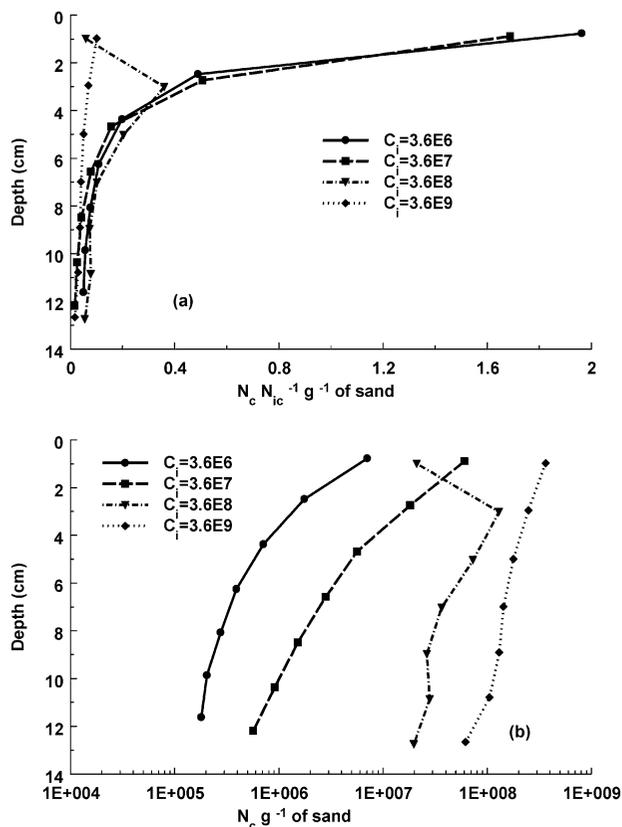


FIGURE 5. Final colloid retention profiles for $1.1 \mu\text{m}$ CML colloids in $150 \mu\text{m}$ Ottawa sand; $q \approx 0.1 \text{ cm min}^{-1}$, pH 10, IS = 31 mM, and $C_i = 3.6 \times 10^6$, 3.6×10^7 , 3.6×10^8 , and $3.6 \times 10^9 \text{ N}_c \text{ mL}^{-1}$. (a) Relative soil concentrations ($N_c N_{ic}^{-1} \text{ g}^{-1}$) of colloids are plotted as a function of depth from the column inlet. (b) Soil concentration of colloids ($N_c \text{ g}^{-1}$) is plotted on a semilog scale as a function of depth.

value of soil colloid concentration ($S^{\text{max}}, \text{N}_c \text{ M}^{-1}$; M is mass), the geometrically estimated solid surface area of the sand ($A_s, L^2 L^{-3}$; L is length), the cross-sectional area of the colloids ($A_b, L^2 \text{ N}_c^{-1}$), and the soil bulk density ($\rho_b, \text{M L}^{-3}$) as $S_f = (\rho_b A_b S^{\text{max}}) / A_s$. The value of S^{max} in Figure 5b was approximately $3.6 \times 10^8 \text{ N}_c \text{ g}^{-1}$, and this yielded an estimate of $S_f = 2.3\%$. Hence, when IS = 31 mM, only a very small fraction of the solid surface area contributes to retention, and this observation further supports the contribution of pore structure on colloid retention under these conditions.

Bradford and Bettahar (12) observed similar effects of C_i on BTCs and RPs of $1.1 \mu\text{m}$ carboxyl colloids in various sized sands (360, 240, and $150 \mu\text{m}$) when the system pH was approximately 7 and IS was 1 mM. This study applied approximately an equal mass of colloids to each column by adjusting the pulse duration for a particular value of C_i . For the same input mass of colloids, an increasing amount of colloid mass was recovered in the column effluent for higher values of C_i . To confirm this finding, we conducted additional colloid transport experiments when q was 0.25 cm min^{-1} , IS was 31 mM, and C_i was 3.6×10^7 and $3.6 \times 10^8 \text{ N}_c \text{ mL}^{-1}$. In this case, a similar input mass of colloids was injected into a column by adjusting the pulse duration. Figure S4 of the Supporting Information presents colloid BTCs from these experiments. Mass balance information indicates that 85% and 32% of the colloids were recovered in the effluent when C_i was 3.6×10^8 and $3.6 \times 10^7 \text{ N}_c \text{ mL}^{-1}$, respectively. Hence, the effect of C_i on colloid retention was not just a time- and concentration-dependent “filling” process.

The observed concentration effects on the BTCs and RPs shown in Figures 1, 2, 4, and 5, and Figures S3 and S4 of the

Supporting Information are hypothesized to be due to the following reasons: (i) time- and concentration-dependent filling of retention sites and (ii) concentration-dependent mass transfer of colloids to retention sites. Mass transfer to low velocity regions with enhanced retention was observed in the micromodel experiment to occur by advective and dispersive fluxes in the aqueous phase and rolling and sliding along on the solid surface. The collector efficiency (relative mass transfer of colloids to collector surfaces) is predicted to be independent of input concentration according to the filtration theory (40). Conversely, quantitative evaluation of mass transfer of colloids along the collector surface via rolling and/or sliding has not received much research attention. Higher input concentrations are expected to produce less relative mass transfer to retention locations due to increased numbers of collisions that knock weakly associated colloids off the solid phase. This hypothesis is supported by the observed dependence of BTCs on C_i (number of collisions) and adhesive and fluid drag forces (an optimal value for rolling mass transfer will depend on IS, pH, and q). Micromodel observations also support this conceptual picture.

Results from this study have important implications for predicting the fate of colloids and microorganisms and colloid-associated contaminants in subsurface environments that are unfavorable for attachment. Specifically, results indicate that only a small fraction of the porous media may contribute to colloid retention, and that once this fraction is filled, then enhanced transport of colloids is likely. Hence, conclusions about the fate of colloids that are derived from transport experiments conducted under clean bed initial conditions or without equilibration with natural background colloids are unlikely to accurately reflect their true long-term transport potential. Furthermore, clean bed transport experiments under unfavorable attachment conditions are expected to be very sensitive to the suspension concentration (including natural background levels), and caution is therefore warranted when comparing with results in other conditions.

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Supporting Information Available

A brief description and discussion of (i) the protocol for the packed column and micromodel experiments, (ii) information on replicate column experiments (Table S1 and Figure S1), (iii) a colloid BTC and RP following a decrease in the IS from 31 to 6 mM and two flow interruptions during the elution phase (Figure S2), (iv) additional BTCs for transient C_i experiments (Figure S3), and (v) a comparison of colloid BTCs that apply similar input mass of colloids at different C_i values by adjusting the pulse duration (Figure S4). This material is available free of charge via the Internet at <http://pubs.acs.org>.

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